

Chopping and Limitations to MEBT

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Fermilab

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- Beam Dump

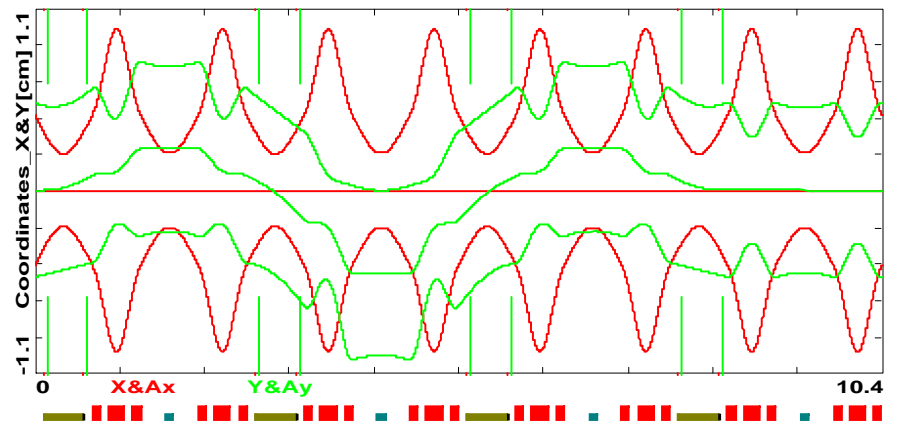
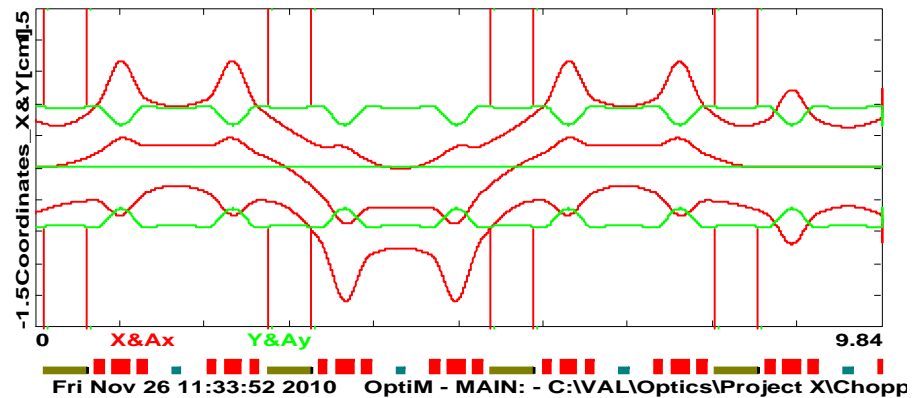
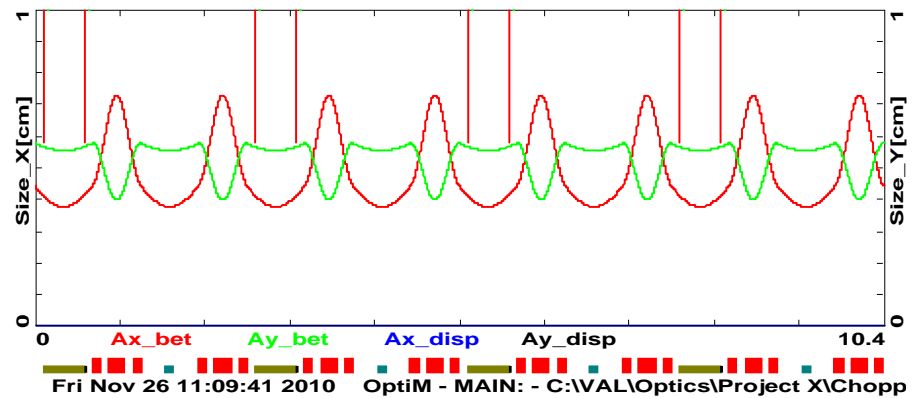
Project X Meeting
November 30, 2010

MEBT Optics

- Here and below we assume:
 - ◆ $\epsilon_{n_rms}=0.2$ mm mrad
 - ◆ The beam collimator is located at $x(y)=0$
 - ◆ The scrapers are located at 3σ

Case without RF cavities

- Looks great
 - ◆ Perfectly periodic beam envelopes
- Vertical kick requires less voltage and therefore is preferable !!!



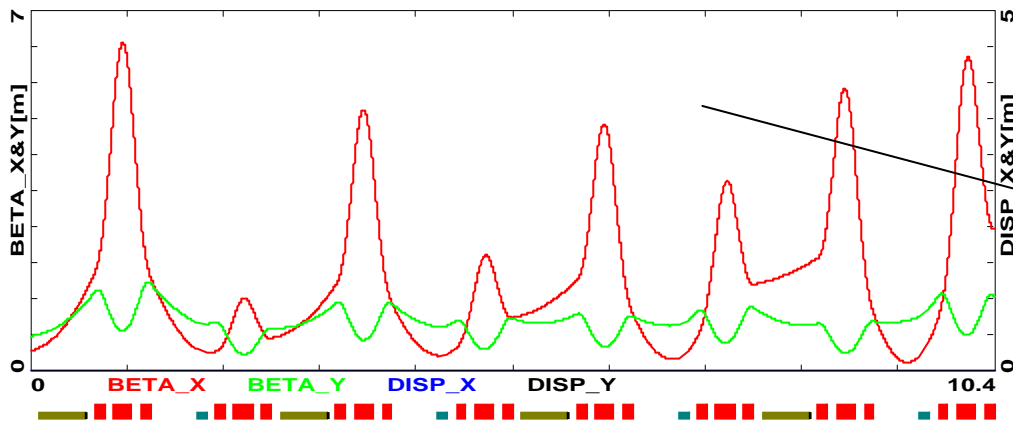
*3 σ beam size in absence of cavity focusing;
 H kick ± 200 V, gap ± 5.8 mm, $G=0.449$ kG/cm;
 V kick ± 160 V, gap ± 7.5 mm, $G=0.585$ kG/cm.*

MEBT Optics (continue)

Effect of RF cavities

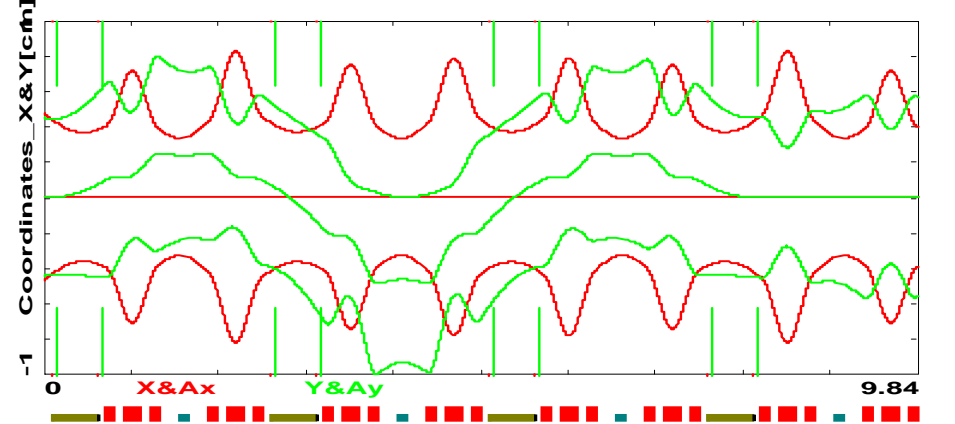
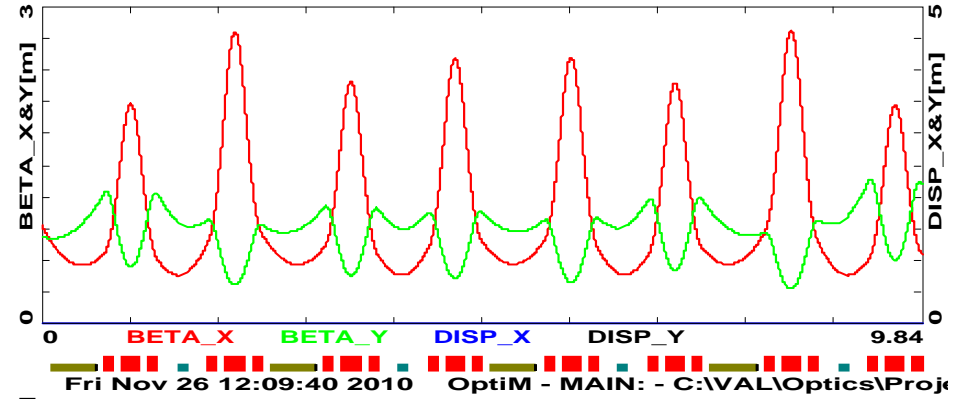
- Cav. \perp focusing destroys the optics periodicity
- For $f_{RF}=325$ MHz & $\mu_L=90$ deg
 - ◆ Cavity focusing: $F=-260$ cm
- RF cavities have to be moved from centers of RF straights to make space for beam dump
- It strongly amplifies β_x beating

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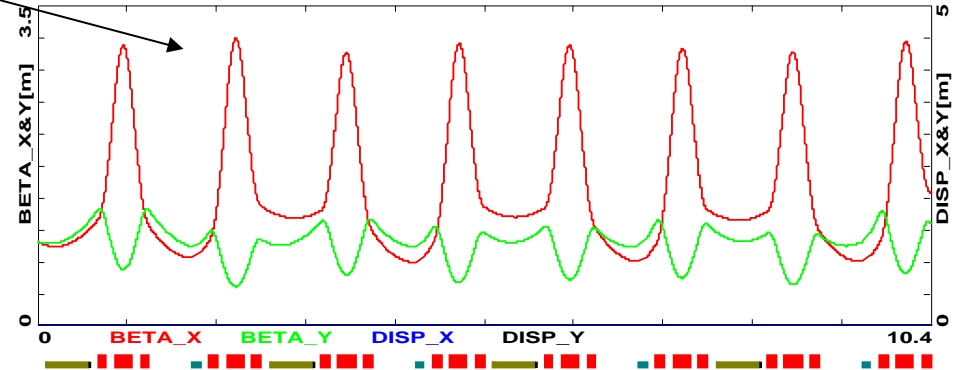
- Optics correction results in 2 times reduction of β_{Xmax}

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*Symmetr. cav. pos.: 3σ beam size in absence of cavity focusing; $G_F=0.522$ & $G_D=0.595$ kG/cm
 $\mu_x=\mu_y=2.01$ V kick ± 170 V, gap ± 6.33 mm,*

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Asymmetric cavity location

MEBT Optics (continue)

- Correction of focusing requires
 - ◆ Vertical
 - Three families of defocusing quads
 - ◆ Horizontal
 - Each focusing quad is regulated independently

Major parameters of MEBT

Beam energy	2.5 MeV
Beam current	5 mA
Longitudinal rms emittance	1 $\mu\text{eV s}$
Normalized rms \perp emittance	0.2 mm mrad
Norm. emittance ratio: $\varepsilon_L/\varepsilon_\perp$	1.6
Longitudinal phase advance	90 deg (per 2 cells)
Transverse phase advance	\sim 90 deg (per 1 cell)
Bunch (RFQ) frequency	162.5 MHz
RF frequency	325 MHz
RF voltage	41 kV

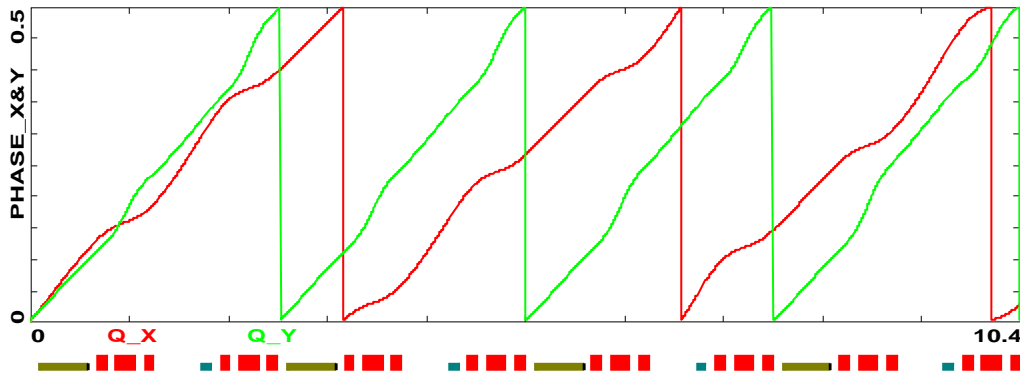
Quad parameters

Name	L[cm]	G[kG/cm]
qD	10	-0.5308
qF1	20	0.4558
qD1	10	-0.5408
qD2	10	-0.6378
qF2	20	0.4698
qD	10	-0.5308
qD	10	-0.5308
qF3	20	0.4438
qD1	10	-0.5408
qD2	10	-0.6378
qF4	20	0.4718
qD	10	-0.5308
qD	10	-0.5308
qF5	20	0.4438
qD1	10	-0.5408
qD2	10	-0.6378
qF6	20	0.4718
qD	10	-0.5308
qD	10	-0.5308
qF7	20	0.4448
qD1	10	-0.5408
qD2	10	-0.6378
qF8	20	0.4558
qD	10	-0.5308

MEBT Optics with space charge

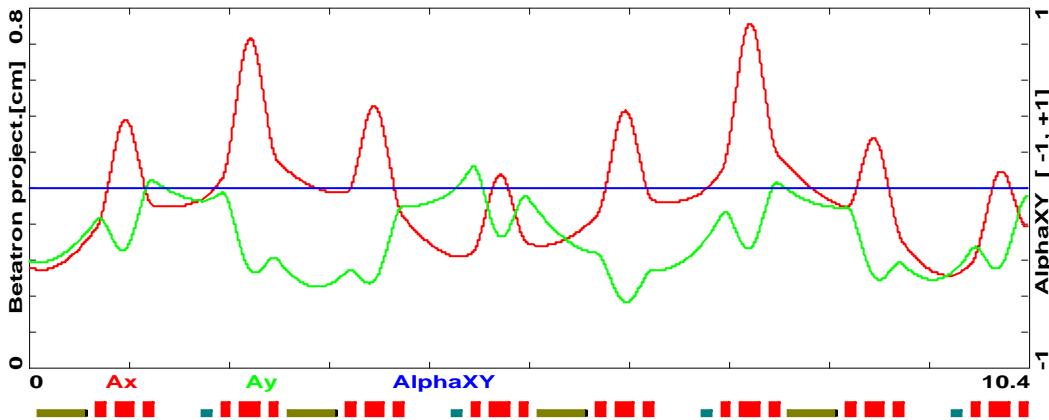
Without space charge: $\mu_x \approx \mu_y \approx 90^\circ$

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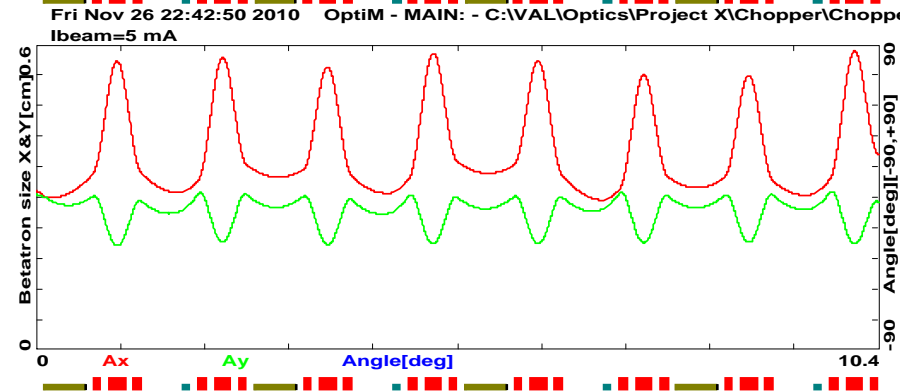
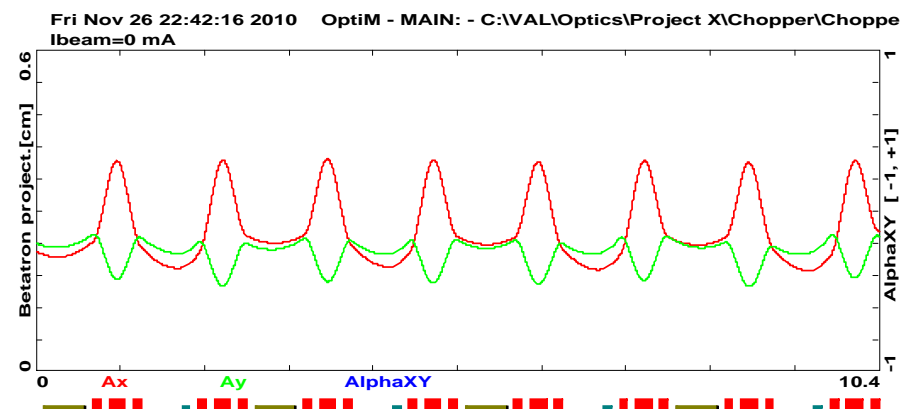


If not tuned the space charge yields large beam envelope oscillations

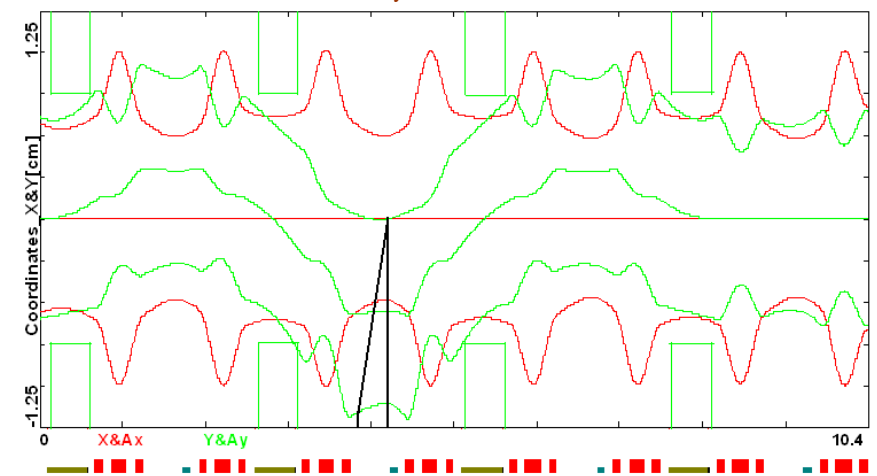
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Matching at MEBT entrance strongly suppresses the oscillations



*Beam envelopes $\sqrt{2}\sigma$ for
0 mA - top, 5 mA bottom*



*3σ beam envelopes; 0 mA scaled to 5 mA
V kick ± 230 V, gap ± 7.4 mm,*

MEBT Optics (continue)

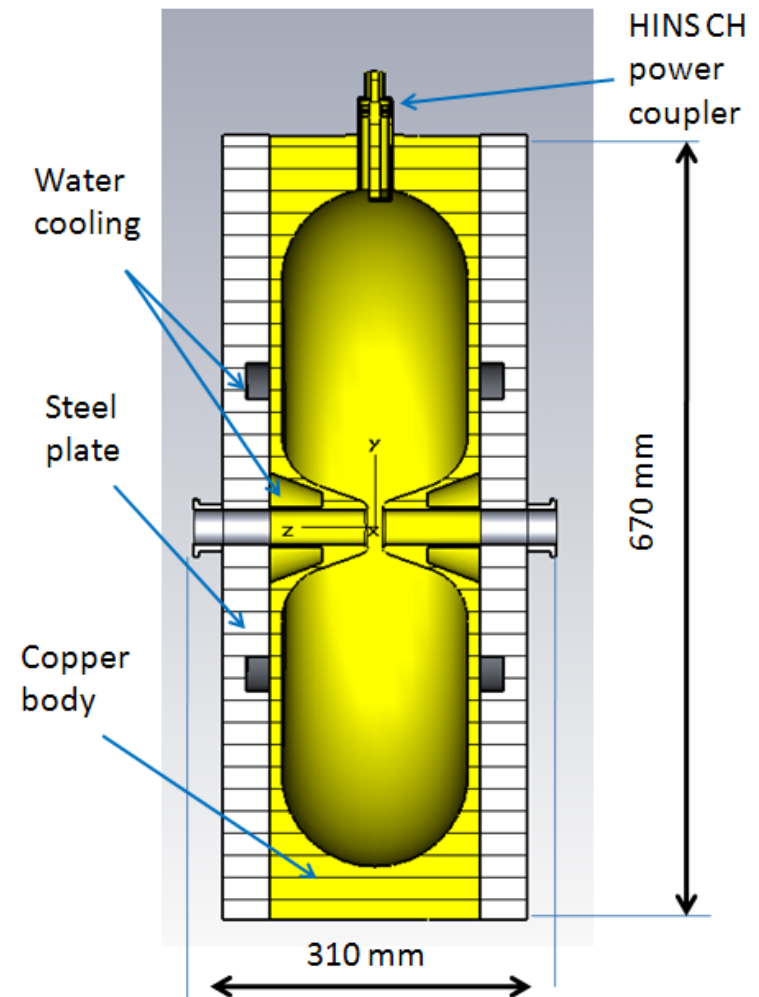
■ Period structure

Name	qD	drift	qF	drift	qD	drift
Length [cm]	10	10	20	10	10	70

- ◆ Quads: $G < 0.7$ kG/cm; aperture: $\varnothing = 4$ cm, $B_{\text{tip}} < 1.4$ kG

■ RF cavities

- ◆ 325 MHz looks good if the longitudinal emittance $\leq 1 \mu\text{eV s}$
 - $\sigma_{\phi_{\text{max}}} = 18$ deg
@ $1 \mu\text{eV s}$ & $I_{\text{beam}}=0$
- ◆ Period 260 cm, $V=41$ kV, $\mu_L=90$ deg.
 - Larger emittance will require 162.5 MHz cavities with 2 times larger voltage (~ 82 kV)
 - For the same μ_L the low frequency RF will have the same effect on transverse focusing

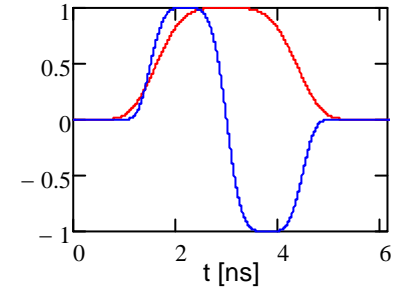


Summary for MEBT optics

- Kicker requirements: $L=50$ cm, $V_{eff}=\pm 250$ V, gap 15 mm
 - ◆ Almost 2 times reduction of kicker voltage is related to
 - Using vertical kick instead of horizontal - 1.25 times
 - Reduction of emittance from 0.4 to 0.2 mm mrad ~ 1.4 times
 - ◆ Space charge increases the beam size
 - \Rightarrow required kick grows by 1.35 times from 0 to 5 mA (170 \rightarrow 230 V)
- Beam dump - large beam power (up to 12.5 kW)
 - ◆ Allocated space for RF cavity and beam dump is 70 cm
 - ◆ It is tight
 - Can be alleviated by shortening quads \Rightarrow total length of triplets
 - a design is required to see how much can be gained

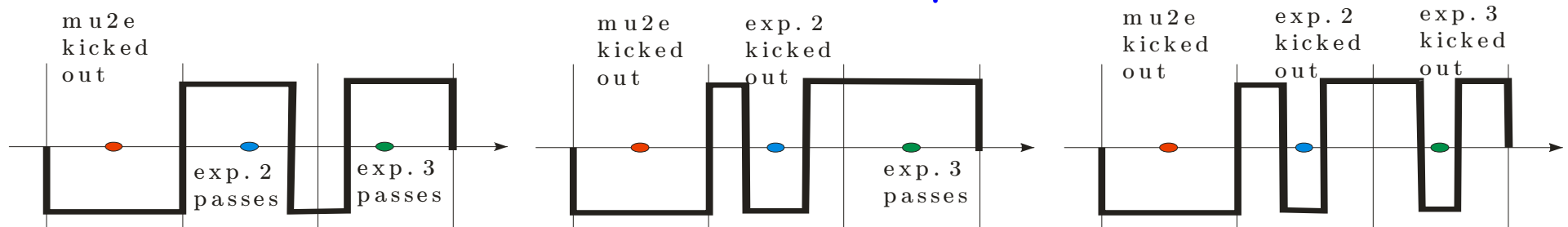
■ Bipolar kicks: "+" - no chop; "-" - chop; "0" - half bunch chop

- ◆ It allows the beam current regulation
- ◆ It reduces the voltage of power amplifier by 2 times
- ◆ Allows to use an amplifier without DC coupling but requires twice larger bandwidth
 - Absence of DC coupling => effective protection of kicker overheating by the beam halo with detecting DC current



■ Longitudinal tails of RFQ can limit the beam extinction

- ◆ It can be addressed by pulse shape adjustments for one experiment (mu2e) but can be done for all experiments
- ◆ It will be easier for a single polarity (entire bucket) kick
- ◆ Simulations are needed to make a quantitative conclusion



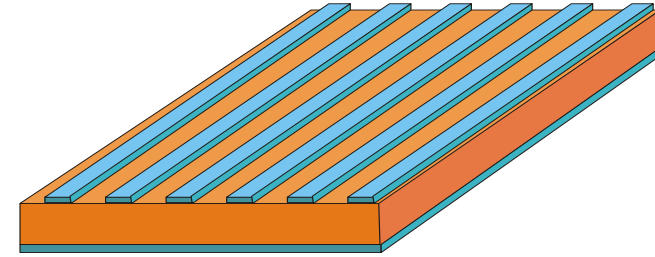
Bunch-by-Bunch Kickers

- 4 kickers: $L=50$ cm ($2*25$ cm) , $U_{\text{eff}}=\pm 250$ V (gap 15 mm)
- 6.1 ns between bunches
 - ⇒ Bunch-to-bunch distance 13.4 cm
 - ⇒ Bandwidth ~ 0.3 GHz for bipolar kicks
 - ⇒ The pulse velocity should match the beam velocity
- There are 3 ways to decelerate the wave
 - ◆ Spiral (old GHz scopes)
 - ◆ Meander (CERN proposal)
 - ◆ short kickers connected by a coaxial delay lines
- The major reasons limiting the bandwidth are
 - ◆ coupling between stripes
 - ◆ reflections from discontinuities
 - ◆ losses in the conductor and dielectric

Simple analytical model for signal propagation

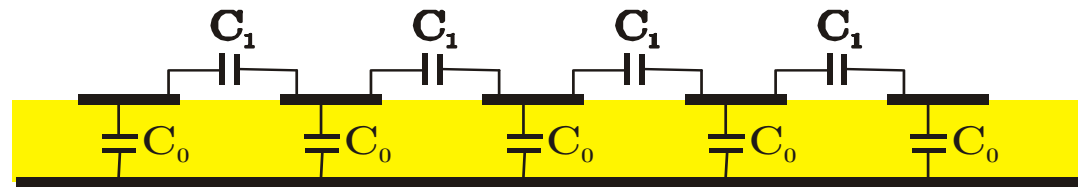
- In the absence of coupling between nearby lines it can be considered as a transmission line

- ◆ Dispersion is small
 - Dominated by loss in the conductor



- Equations for parallel lines (coupling is on)

$$\begin{cases} \frac{\partial I_n}{\partial x} = -C_0 \frac{\partial U_n}{\partial t} + C_1 \left(\frac{\partial U_{n+1}}{\partial t} + \frac{\partial U_{n-1}}{\partial t} \right) \\ \frac{\partial U_n}{\partial x} = -L_0 \frac{\partial I_n}{\partial t} \mp L_1 \left(\frac{\partial I_{n+1}}{\partial t} + \frac{\partial I_{n-1}}{\partial t} \right) \end{cases}$$



sign “-” if currents in nearby lines go in the same direction, “+” - otherwise
 C_0 and L_0 are capacitance and inductance per unit length; n - numerates lines

- If the same signals are propagated simultaneously in all lines the propagation speed is the same as in a single line

⇒ In the first order of perturbation theory the inductive and capacitive coupling coefficients are

equal $\kappa = \frac{C_1}{C_0} = \frac{L_1}{L_0}$

Coupling between stripes

- Capacitance per unit length of a single stripe is (Gelmont, et.al.,1995)

$$C_0 \approx \frac{1+\varepsilon}{2} \begin{cases} \left[\ln \left(\frac{\sqrt{\cosh(\alpha(b, w, \varepsilon)) + 1}}{\sqrt{\cosh(\alpha(b, w, \varepsilon)) - 1}} \right) \right]^{-1}, & \tanh(\alpha(b, w, \varepsilon)) \leq 1/\sqrt{2}, \\ \frac{1}{\pi^2} \ln \left(2 \frac{\sqrt{\cosh(\alpha(b, w, \varepsilon)) + \sqrt{\sinh(\alpha(b, w, \varepsilon))}}{\sqrt{\cosh(\alpha(b, w, \varepsilon)) - \sqrt{\sinh(\alpha(b, w, \varepsilon))}} \right), & \tanh(\alpha(b, w, \varepsilon)) \geq 1/\sqrt{2}, \end{cases}$$

$$\alpha(b, w, \varepsilon) = \frac{\pi w \varepsilon}{4b(1+\varepsilon)}.$$

- for $w \ll b, h$ it can be simplified

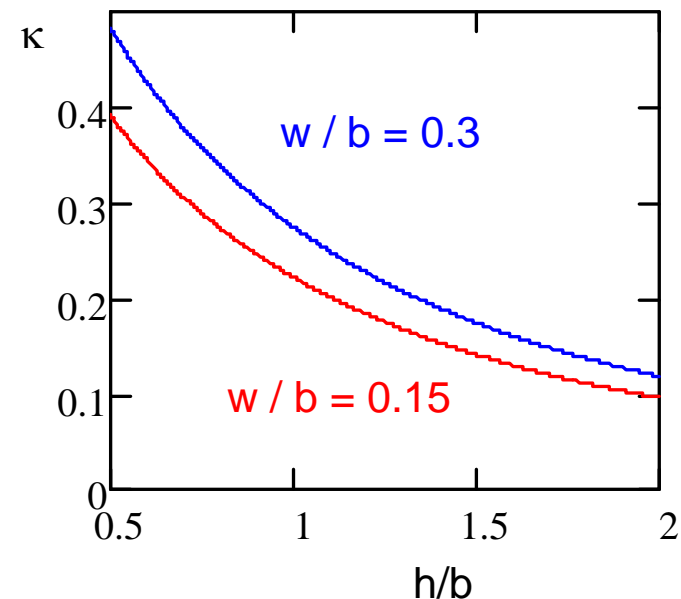
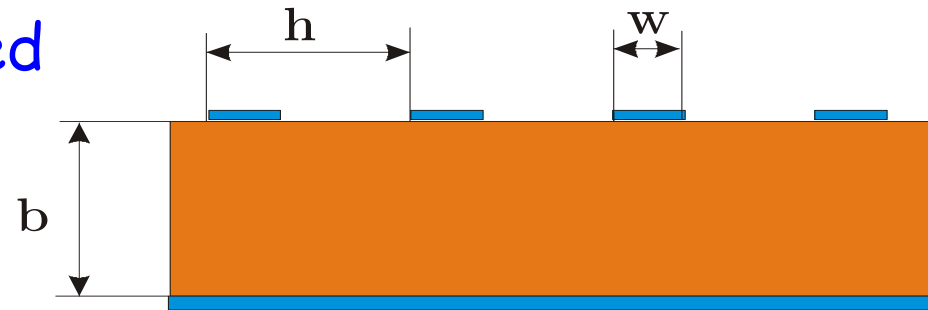
$$C_0 \approx \frac{\varepsilon + 1}{4} \left[\ln \left(\frac{16 \varepsilon + 1}{\pi} \frac{b}{\varepsilon w} \right) \right]^{-1}, \quad L_0 = \frac{2}{c^2} \ln \left(\frac{32b}{\pi w} \right)$$

- Then, the coupling coefficient is

$$\kappa \approx \ln \left(\sqrt{1 + (2b/h)^2} \right) / \ln \left(\frac{32b}{\pi w} \right), \quad w \ll b, h$$

- A desire to have good kicker efficiency ($U_{eff} \geq 0.7U_0$) requires $h \leq b$

$$\Rightarrow \kappa \geq 0.15$$



Coiled kicker

Looking for a

solution in the form:

$$\begin{pmatrix} U(s,t) \\ I(s,t) \end{pmatrix} = \begin{pmatrix} U_0 \\ I_0 \end{pmatrix} e^{i(\omega t - kx)}$$

and taking into account

the boundary condition:

$$\begin{cases} U_{n+1}(s,t) = U_n(s+l,t) \\ I_{n+1}(s,t) = I_n(s+l,t) \end{cases}$$

one obtains the dispersion equation

$$k \approx \sqrt{\varepsilon} \frac{\omega}{c} \left[1 + 8\kappa^2 \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \sin^2\left(\sqrt{\varepsilon} \frac{\omega l}{2c}\right) \right]$$

l - length of a single turn

ε - is dielectric permittivity (assume $\varepsilon \gg 1$)

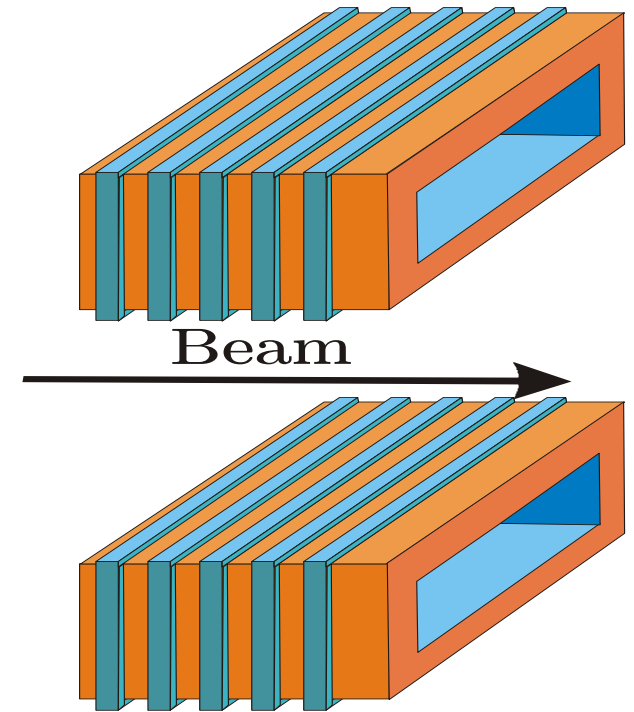
Impedance of the line is frequency dependent too

$$Z(\omega) \approx Z_{line} \left[1 + 2\kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right], \quad Z_{line} = Z_0 \frac{\sqrt{\varepsilon}}{4\pi C_0}$$

Reflections modulate the wave amplitude propagating along beam

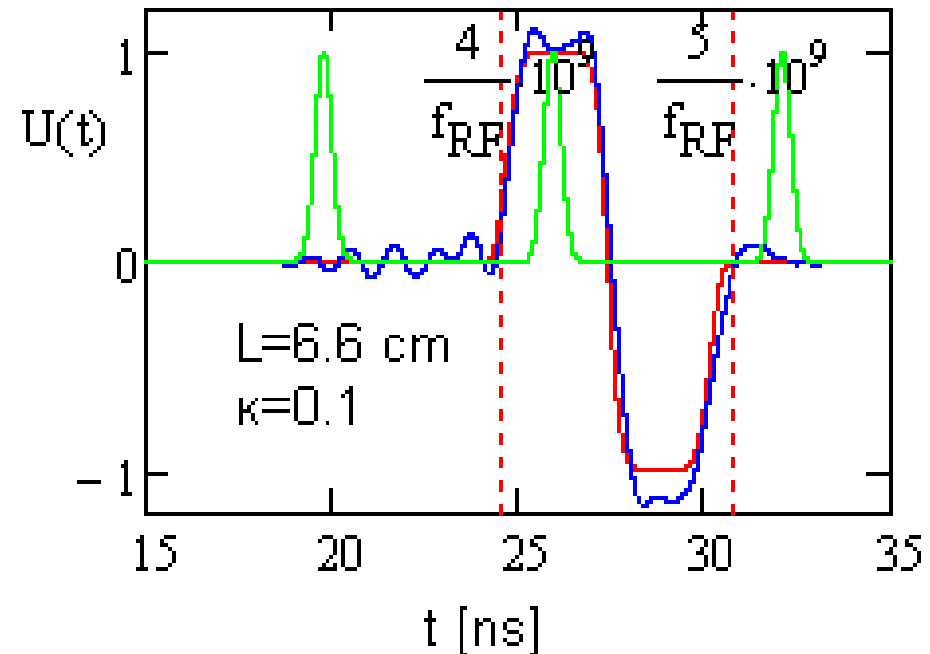
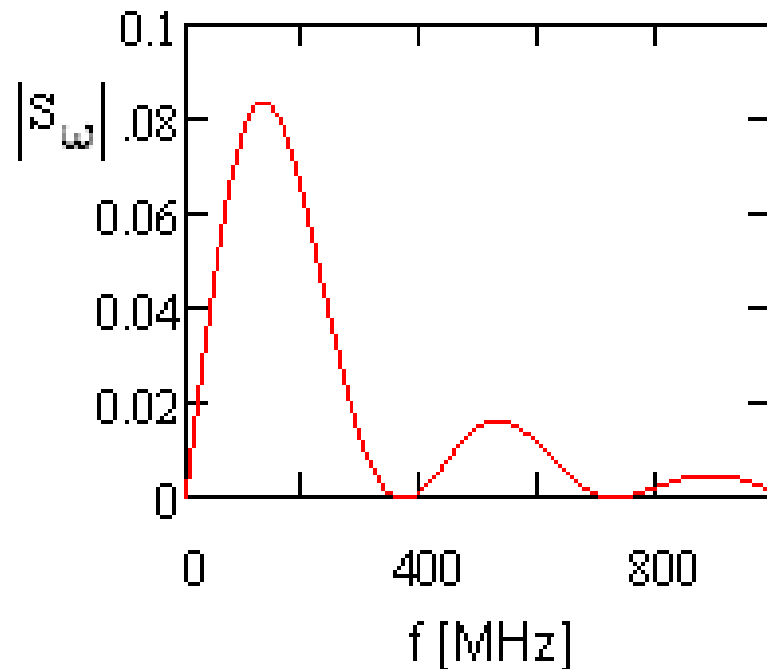
$$U(\omega) \approx U_0 \left[1 + \kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right]$$

Wave reflected from termination weakly interacts with beam



Coiled kicker (continue)

- Phase modulations, $\exp(-ik(\omega)s)$, affect the pulse propagation stronger than the wave reflections from the kicker due to frequency dependent mismatch
 - ◆ Damping due to finite resistivity makes only small correction



turn length - $l=6.6 \text{ cm}$, $\kappa = 0.1$, $\varepsilon=3.5$, $h=9 \text{ mm}$, total length - 50 cm

- Coupling coefficient was set to obtain sufficiently small pulse distortions
 - ◆ $\kappa \leq 0.1 \Rightarrow$ large distance between turns \Rightarrow large kick attenuation
 - Reduction of one turn length would help but is limited by kicker width (i.e. beam size)
 - ◆ Therefore the coiled kicker does not look promising

Meander kicker

Looking for solution in the form:

$$\begin{pmatrix} U(s,t) \\ I(s,t) \end{pmatrix} = \begin{pmatrix} U_1 e^{-ik_n x} + U_2 e^{ik_n x} \\ I_1 e^{-ik_n x} + I_2 e^{ik_n x} \end{pmatrix} e^{i(\omega t - mn)}, \quad k_n = \begin{cases} |k|, & \text{odd } n \\ -|k|, & \text{even } n \end{cases}$$

and taking into account the boundary condition:

$$\begin{cases} U_n(l/2, t) = U_{n+1}(l/2, t) \\ I_n(l/2, t) = I_{n+1}(l/2, t) \end{cases}$$

one obtains the dispersion equation

$$\mu(\omega) \approx \sqrt{\varepsilon} \frac{\omega l}{c} - \kappa \sin\left(2\sqrt{\varepsilon} \frac{\omega l}{c}\right)$$

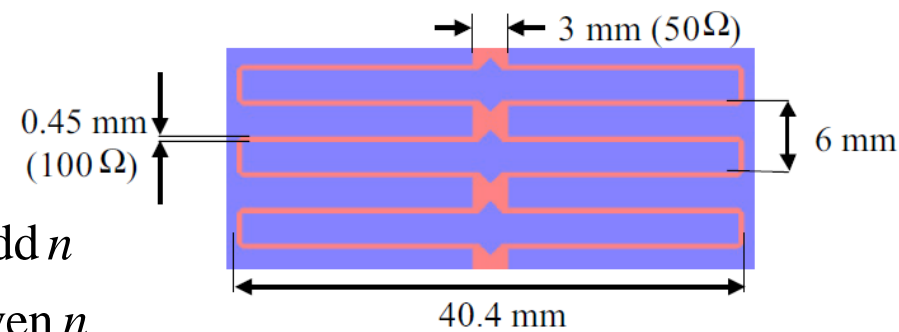
l - length of a stripe (kicker half width)

ε - is dielectric permittivity (assume $\varepsilon \gg 1$)

In the first order the line impedance and wave reflections are the same as for coiled kicker

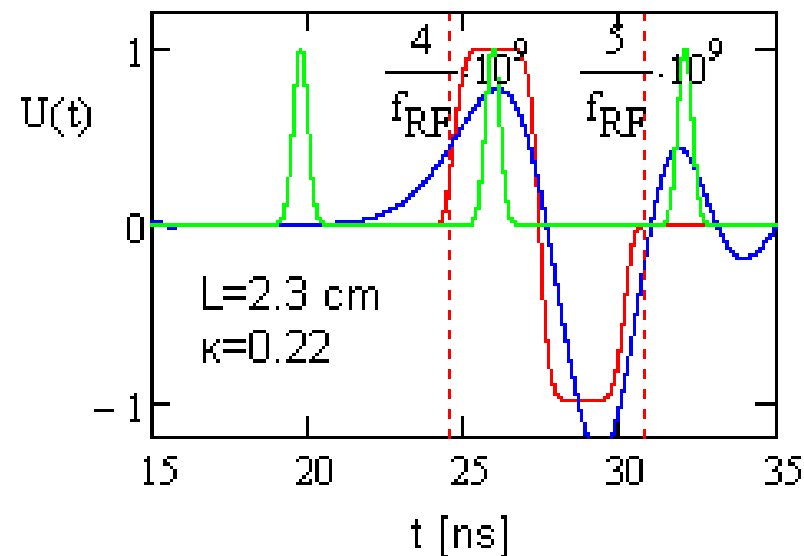
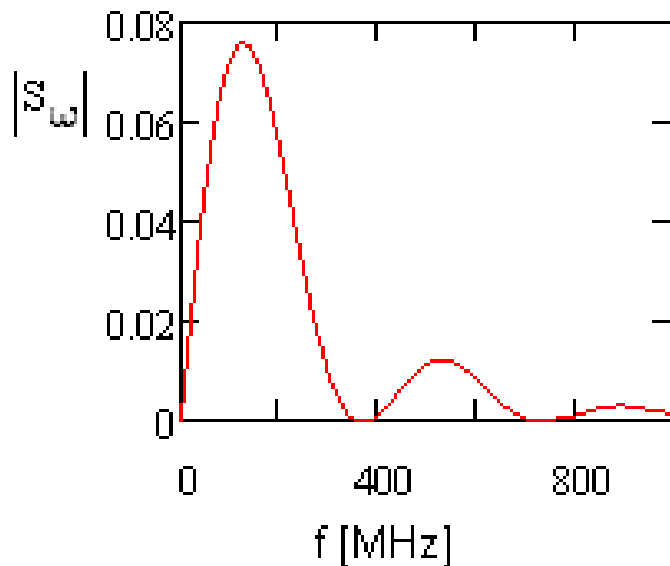
$$Z(\omega) \approx Z_{line} \left[1 + 2\kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right], \quad Z_{line} = Z_0 \frac{\sqrt{\varepsilon}}{4\pi C_0}$$

$$U(\omega) \approx U_0 \left[1 + \kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right]$$



Meander kicker (continue)

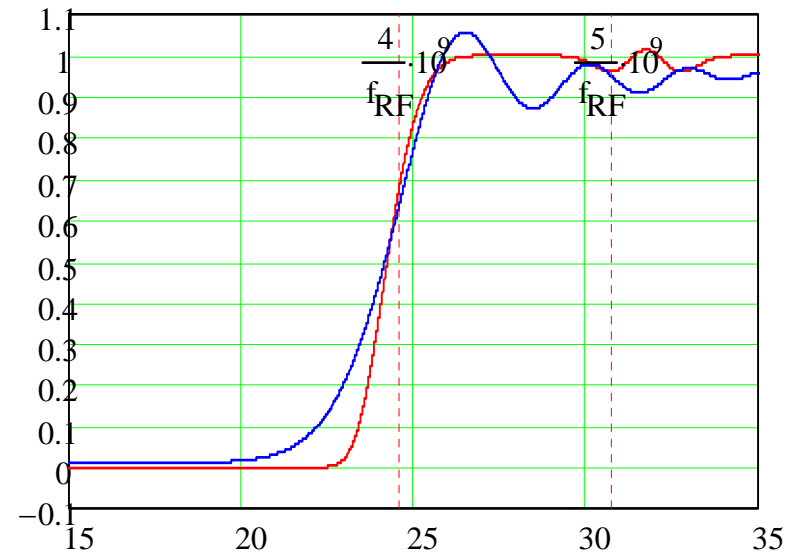
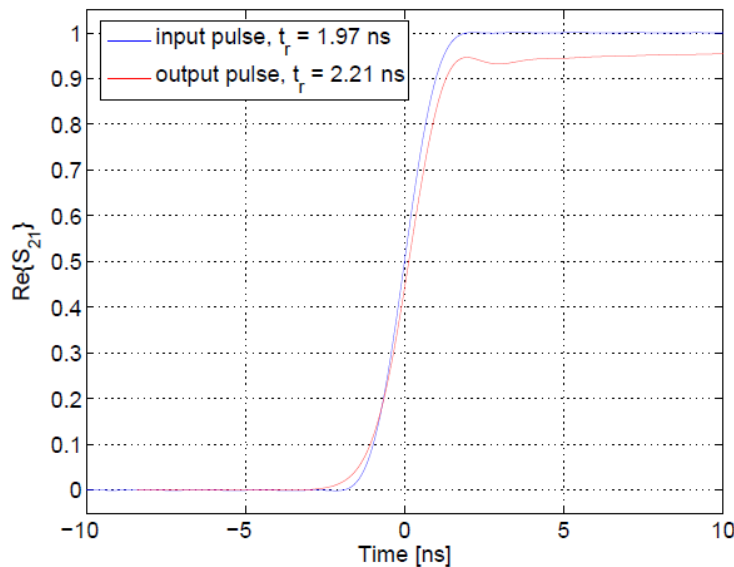
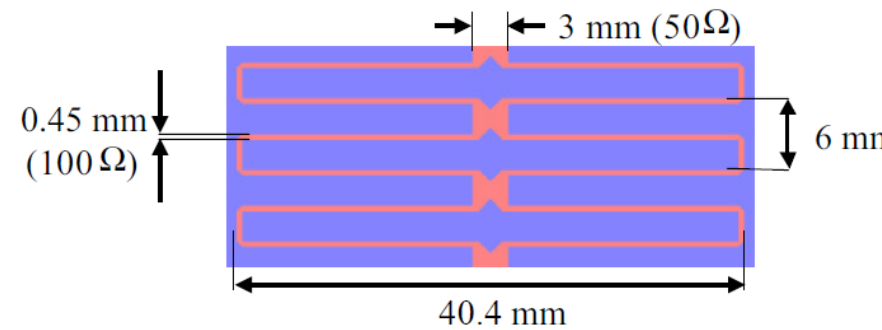
- The same as for coiled kicker the wave reflected from termination weakly interacts with beam
- Not as for coil kicker the dispersion correction is $\propto \kappa$, not to κ^2
 - ◆ i.e. much larger effect for the same coupling
- However much shorter period (more than 4 times) helps
 - ◆ It moves problems to higher frequencies
- Still looks that it does not address Project X needs



*Pulse spectrum and propagation for the CERN kicker proposal adjusted to project X needs,
 $L_{tot}=50$ cm, $h = b = 3$ mm, $l = 23$ mm, $\varepsilon = 9.6$*

CERN proposal for meander kicker

- Total kicker length 40 cm
 - ◆ two 100 Ω lines
- Demonstrated rise time ~ 3 ns
 - ◆ They claim 1 ns (definition?)
- The above analytical estimate looks less optimistic (~ 5 ns)
 - ◆ It correctly predicts that the wave propagates faster by 1.9 times because of strip-to-strip coupling
 - $\kappa = 0.19$ - analytical estimate
 - $\kappa = 0.25$ - fitted from wave propagation speed

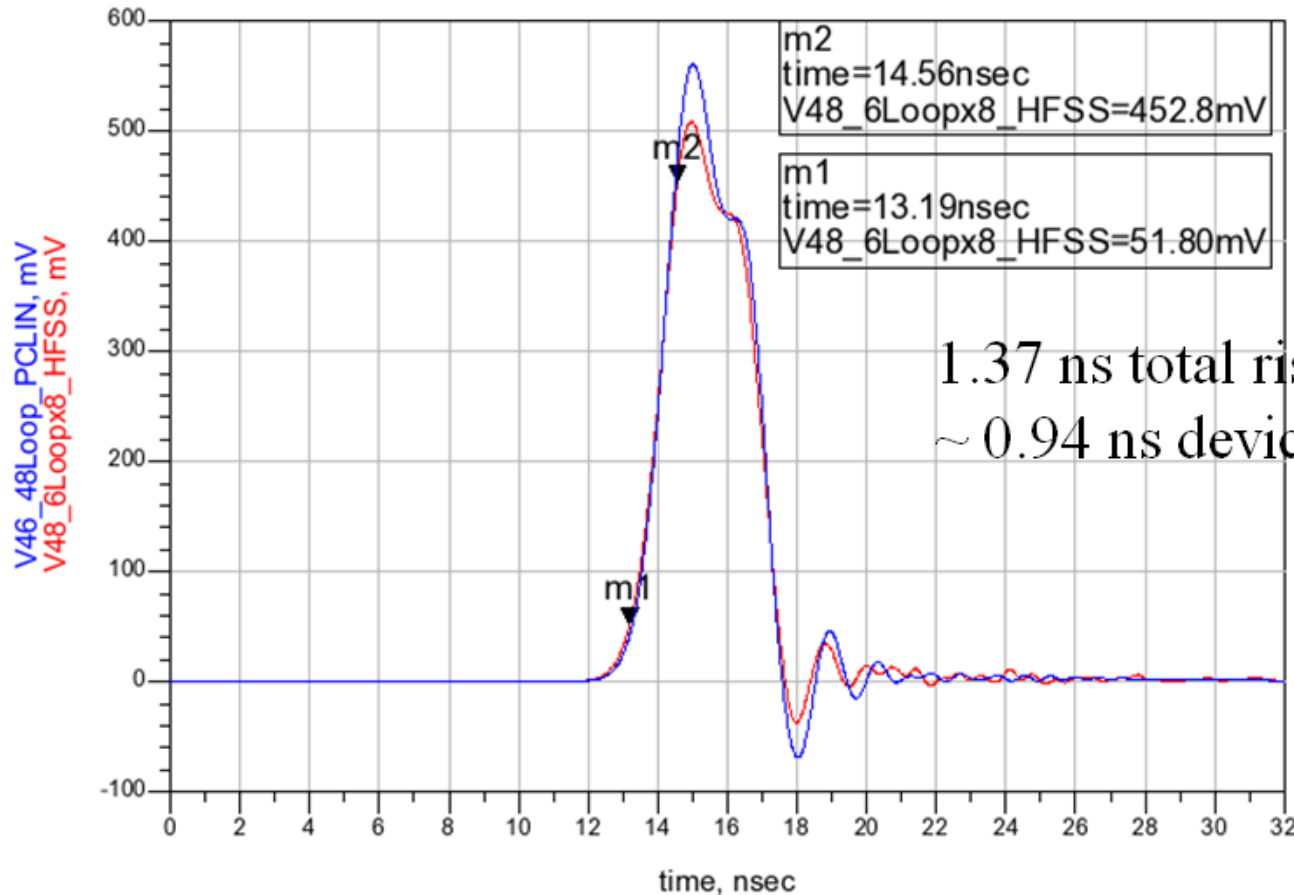


Measured and calculated wave shape at the kicker end

CERN proposal for meander kicker (continue)

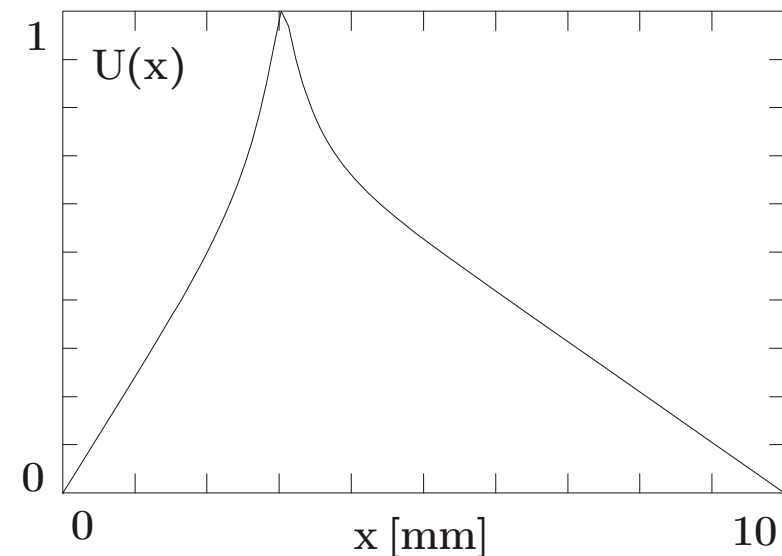
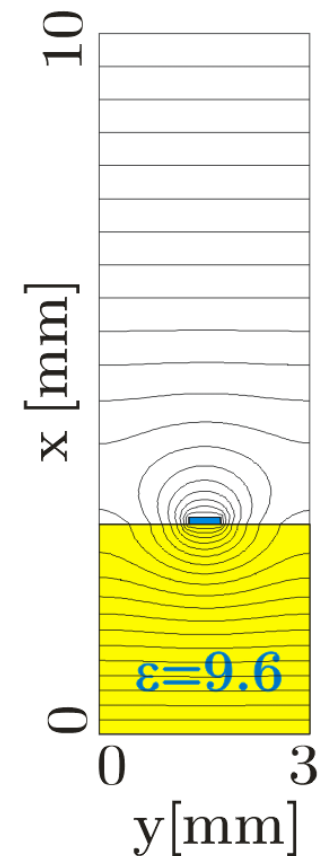
ADS/HFSS 48 CERN Loops

48 Loops (Double Meander), 4 ns pulse



Complications with CERN meander kicker proposal

- Hardly can achieve the desired bandwidth (time resolution)
- Bad kicker efficiency: $\sim 60\%$ ($U_{\text{eff}} \geq 0.6U_0$)
 - ◆ Large ε and $\rho = 100 \Omega$
 - ⇒ small stripe width
 - ⇒ $\sim 30\%$ loss of the kick due to small width
 - ◆ Additional 15% are lost due to stripe resistivity
 - wave damping $\sim 30\%$ to the line end (40 cm)
 - corresponding heating is negligible, $\Delta T \approx 1.5 \text{ C}^\circ$
- Dielectric is directly visible to the beam and can be charged by its tails
 - ◆ Reproducibility???
 - ◆ Discharges can result in a kicker damage



Alternative Approach for Chopper Design (Ding Sun)

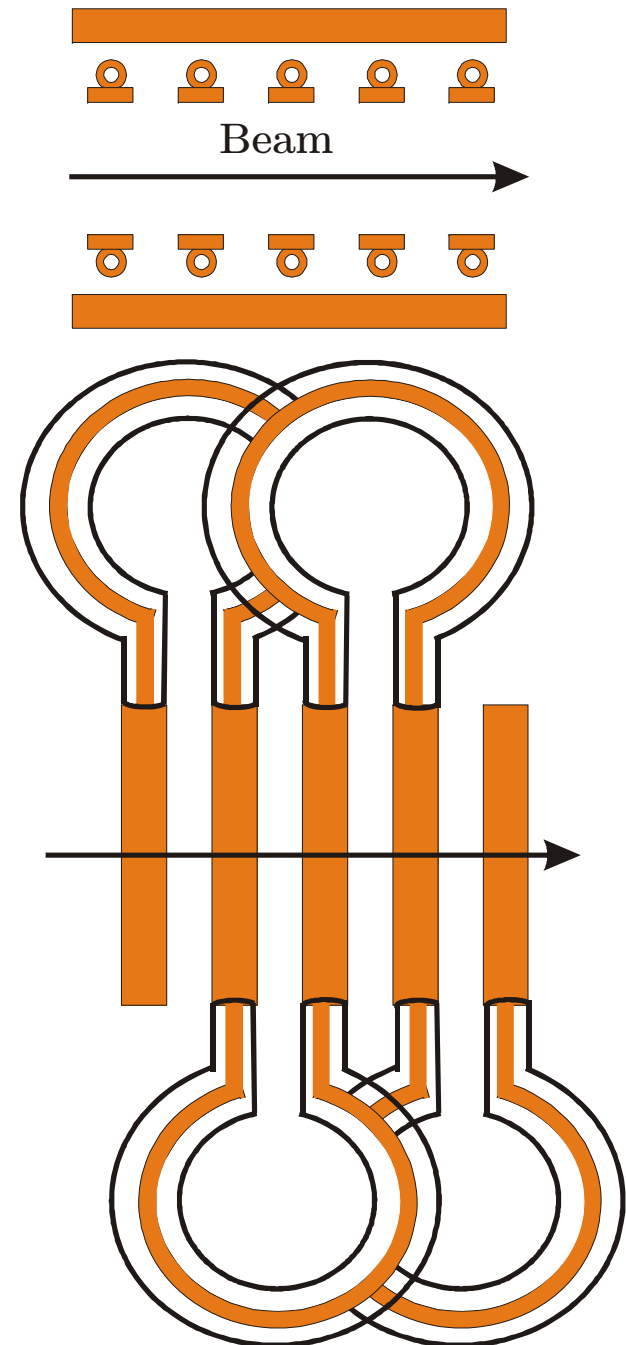
■ Details

- ◆ No dielectric
 - No charging of the surface
- ◆ "RF cable" connection between stripes
- ◆ Smaller effective coupling between lines
- ◆ More effective kicks
- ◆ Water or air cooling of stripes is possible

■ Expected problems

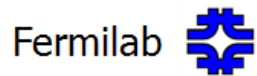
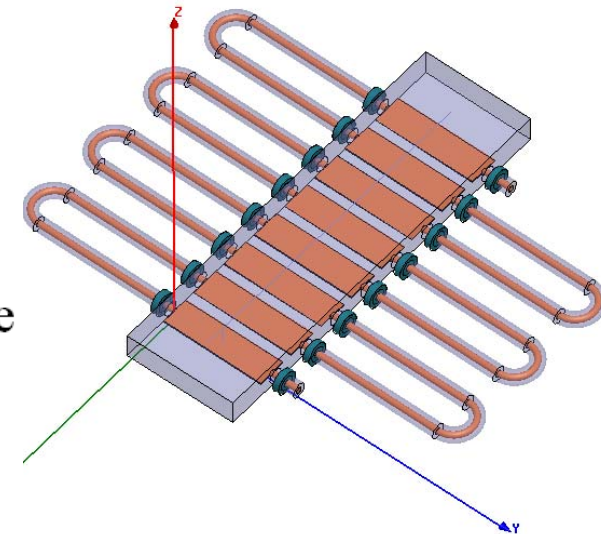
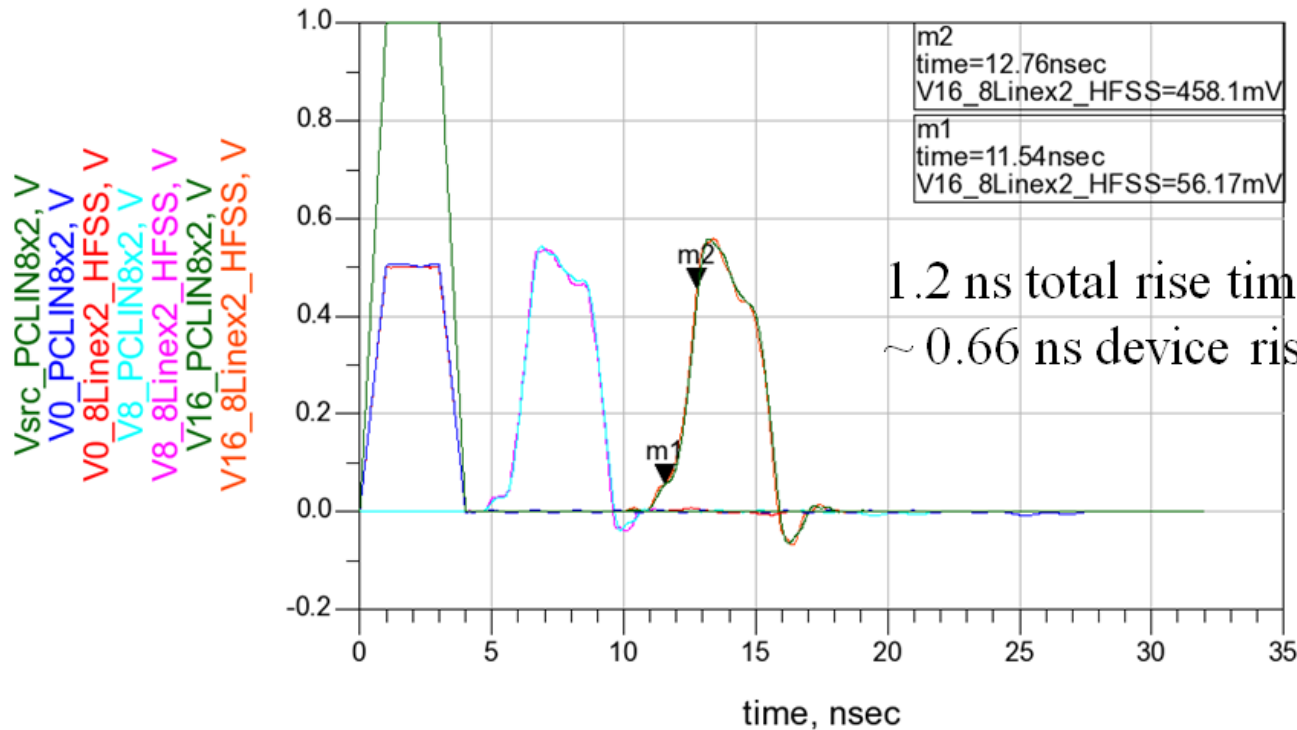
- ◆ Reflections at the transitions

■ Construction of prototype based on the cable delays is started



Alternative Approach for Chopper Design (continue)

16 Striplines, 4 ns pulse / 1 ns rise time



Ding Sun - Project X Meeting

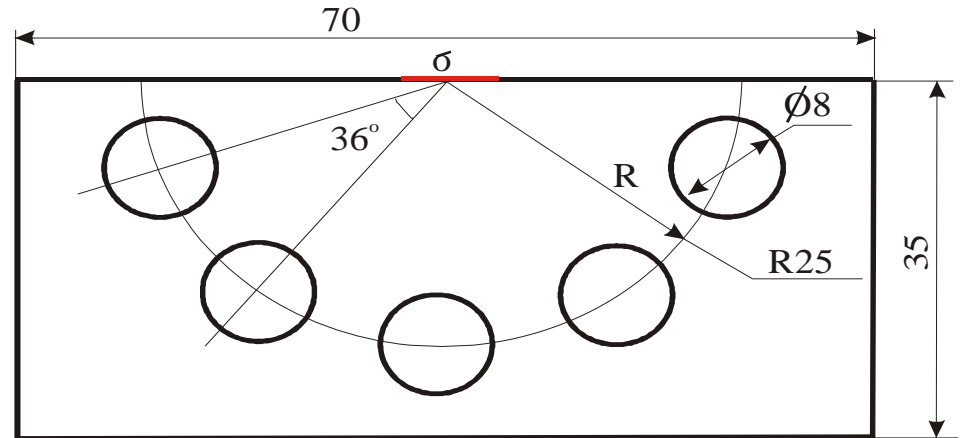
May 4, 2010

Step - 16 mm, total length for the 16 strip-lines kicker is 26 cm, 2 kickers in 1 straight

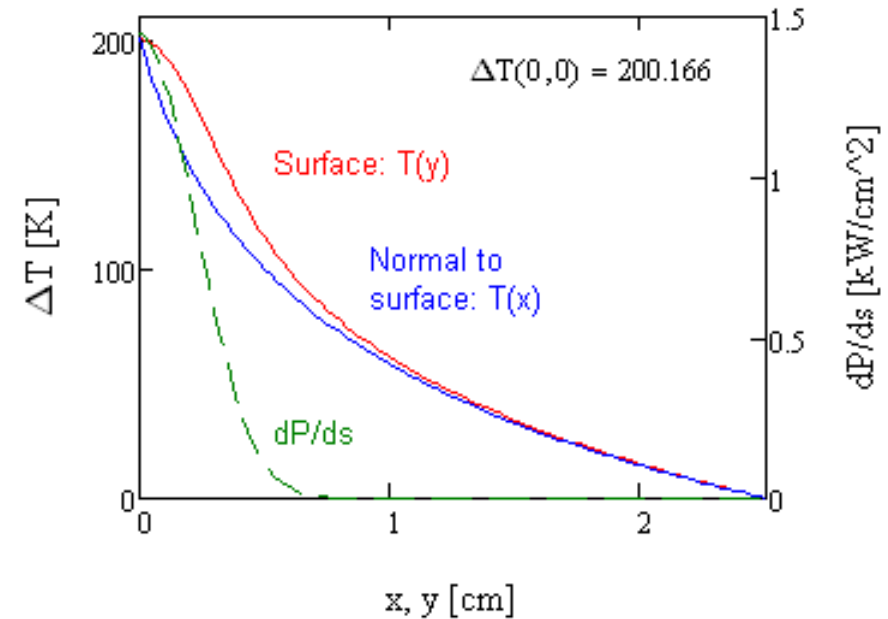
- Rise time is at the boundary of acceptable for double polarity pulse
- Kicker efficiency is much better than for CERN meander
 - ◆ 300 V peak (1 kW) amplifier look adequate for powering one side of the kicker (required effective kicker voltage ± 230 V)
- First tests are expected within 2 months

Beam Dump

- For 5 mA beam the total beam power is 12.5 kW
- Water can accept the power density $dP/ds \leq 60 \text{ W/cm}^2$
 - ◆ Heat removal requires large area of water channels
- Temperature gradient in damp material introduces stresses and should be minimized
- For Gaussian heating profile with $\sigma = 2.2 \text{ mm}$ and the linear power density $dQ/dL = 800 \text{ W/cm}$ the temperature difference in copper $\sim 200 \text{ K}$ ($R = 2.5 \text{ cm}$)



$$\Delta T \simeq \frac{1}{\pi \kappa} \frac{dQ}{dL} \ln \frac{1.89 R}{\sigma}$$



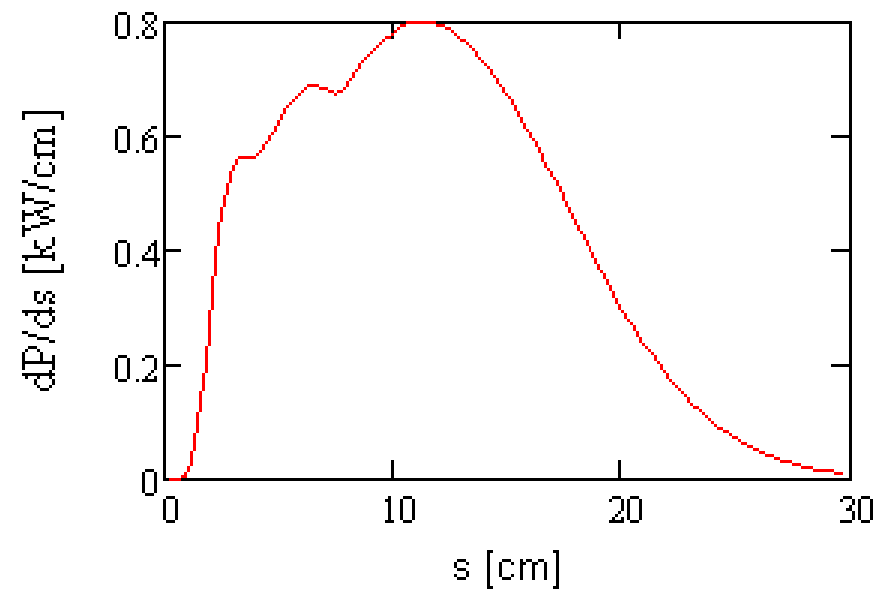
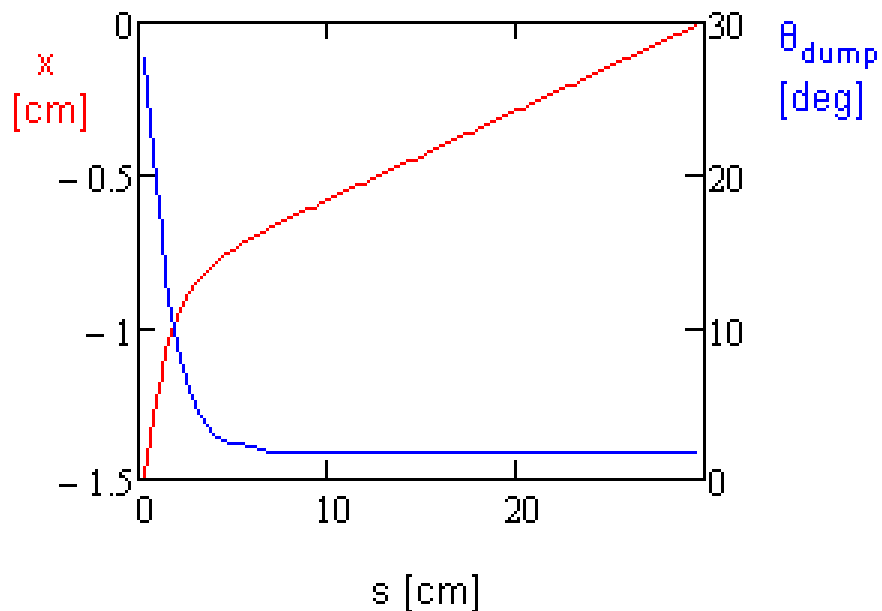
Beam dump (continue)

- Copper looks as a good material due to its high thermal conductivity
- However the temperature difference of 200 K results large stresses
 - ◆ $\Delta T = 40 \text{ K}$ @ stress yield
 - ◆ i.e. we are factor of 5 above stress yield
- The stress can be relieved by deformations
 - ◆ Half of the stress is absorbed by settling material to mean temperature
 - ◆ No significant pulse load
 - $\Delta T = 30 \text{ K}$ for 5 ms interruption
 - Heat penetration (diffusion) rate $\sqrt{dx^2 / dt} \approx 1 \text{ cm}/\sqrt{s}$
 - ◆ Mechanical design should be done to minimize stresses due to dump heating

Length of the beam dump	30 cm
Beam dump angle to beam	29 mrad
Max. linear power density	0.8kW/cm
Water pressure drop	2 atm.
Water pipes connection	serial
Total length of pipes	2 m
Water flow	0.3 l/s
Power density (water-to-Cu)	64 W/cm ²
Water ΔT (inlet-to-outlet)	9.5 C°
ΔT (water-to-Cu)	27 C°
Inlet water temperature	50 C°
Peak temperature	290C°

Beam Dump Space Limitations

- 700 mm drift is allocated for the RF cavity and the beam dump
 - ◆ 300 mm cavity
 - ◆ 300 mm beam dump
 - 3σ scraping
 - Dump face is bend at the entrance to reduce the dump length
 - ◆ 100 mm interfaces



Beam Dump Lifetime

- Proton (H^-) beam destroys the dump surface
 - ◆ Sputtering
 - amplified by oblique incidence - estimate: ~ 0.15 mm/year
 - ◆ Blistering
 - Will be mitigated by high temperature of the dump face
remelting of blistered material - Dump face should look up
- Dump activation and neutron production
 - ◆ Not negligible
 - Would not happen for Cu at $E < 2.1$ MeV or with higher Z material
 - ◆ Sputtering limits usefulness of thin layer of high Z material
 - ◆ Thermal stresses do not allow thick layer
- High speed vacuum pumping is required to keep vacuum in MEBT cavities
- Differential pumping is required to keep good vacuum in SC cavities
- Insulators in dump vicinity have to be protected from the flux of sputtered material

Sputtering estimate

- The beam energy is sufficiently high and small scattering angle approximation can be used
- Using Thomas-Fermi model for calculating the energy transfer to an atom above I_a one obtains the cross section:

$$\sigma \approx \pi r_p^2 Z^2 \frac{(m_p c^2)^2}{I_a E} \left(1 + 0.9 \left(1.174 \frac{Z^{4/3} r_p}{a_0} \frac{m_p c^2}{\sqrt{4 A I_a E}} \right)^{2/3} \right)^{-2}$$

⇒ Sputtering probability per incoming proton - $W \approx \frac{\sigma^2}{a_{lat}^2 \theta}$

$r_p \approx 1.53 \cdot 10^{-16} \text{ cm}$, $a_0 \approx 0.53 \cdot 10^{-8} \text{ cm}$, $m_p c^2 = 938 \text{ MeV}$, $E = 2.5 \text{ MeV}$;

for Cu: $Z = 29$; $A = 65.5$; $I_a = 3.3 \text{ eV}$; $a_{lat} \approx 2.3 \cdot 10^{-8} \text{ cm}$ (atom-to-atom dist.)

⇒ $W = 5.3 \cdot 10^{-3}$ for $\theta = 29 \text{ mrad}$ (1.7 deg)

- There is no reliable exper. data on sputtering by 2.5 MeV prot.
 - ◆ Comparison to simulations points out ~2 times overestimate
 - ◆ for $\theta = 1 \text{ deg.}$: modeling by T. Sizyuk (Purdue univ.) - $W = 4.3 \cdot 10^{-3}$
above estimate - $W = 8.8 \cdot 10^{-3}$
- Applicability condition: incident angle is larger than the scattering angle: $\theta \gg \sqrt{I/E}$ ($\theta \gg 1 \text{ mrad}$)

Conclusions

- Now we better understand requirements to the RFQ beam parameters (emittances, beam current)
 - ◆ RFQ design and simulations will follow
 - ◆ 10 mA RFQ current greatly complicates the beam bump design
 - Looks impossible without liquid metal jet (reliability?) or significant MEBT lengthening with consecutive negative effect on the beam dynamics
- Reduction of transverse emittance and better understanding of optics reduced the kicker voltage to a manageable level, $P \leq 1$ kW
- Present understanding of bunch-by-bunch kickers does not support 352 MHz RFQ (162.5 looks OK)
 - ◆ The choice of the kicker type is not quite clear yet