

# Chopping and Limitations to MEBT

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Fermilab

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- MEBT optics
- Bunch-by-bunch kickers
- Beam Dump

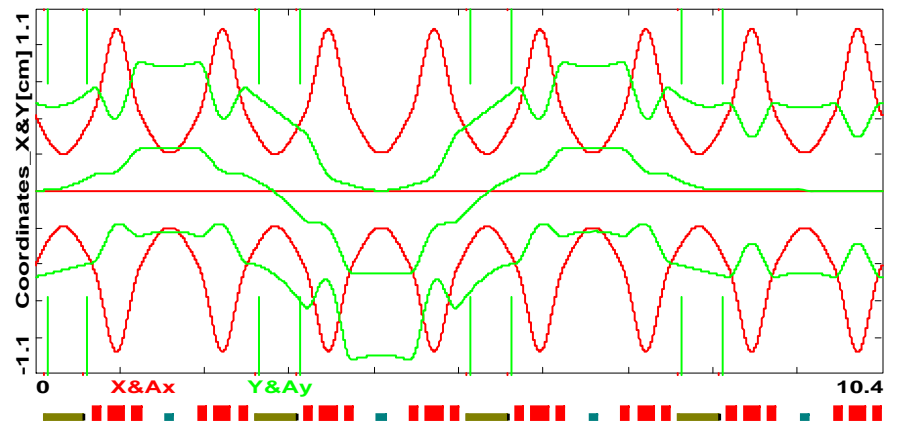
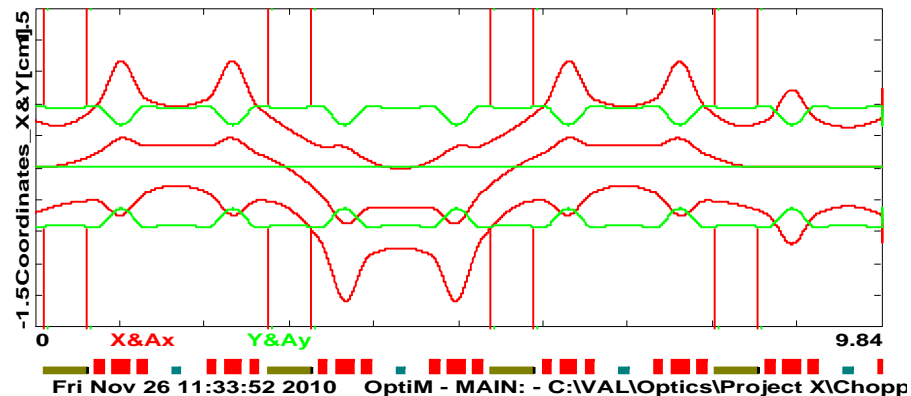
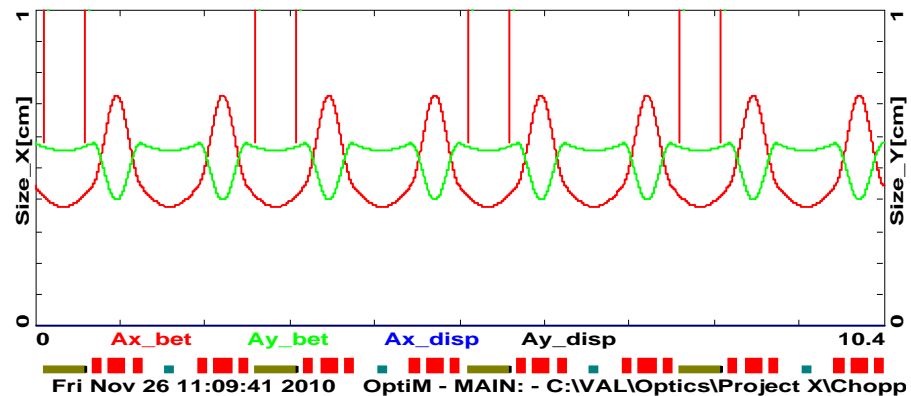
Project X Meeting  
November 30, 2010

# MEBT Optics

- Here and below we assume:
  - ◆  $\epsilon_{n\_rms}=0.2$  mm mrad
  - ◆ The beam collimator is located at  $x(y)=0$
  - ◆ The scrapers are located at  $3\sigma$

## Case without RF cavities

- Looks great
  - ◆ Perfectly periodic beam envelopes
- Vertical kick requires less voltage and therefore is preferable !!!



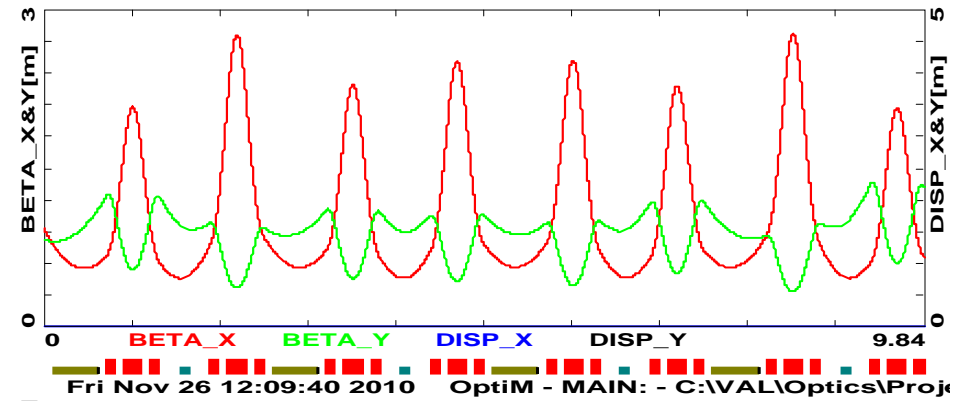
*3 $\sigma$  beam size in absence of cavity focusing;  
 H kick  $\pm 200$  V, gap  $\pm 5.8$  mm,  $G=0.449$  kG/cm;  
 V kick  $\pm 160$  V, gap  $\pm 7.5$  mm,  $G=0.585$  kG/cm.*

# MEBT Optics (continue)

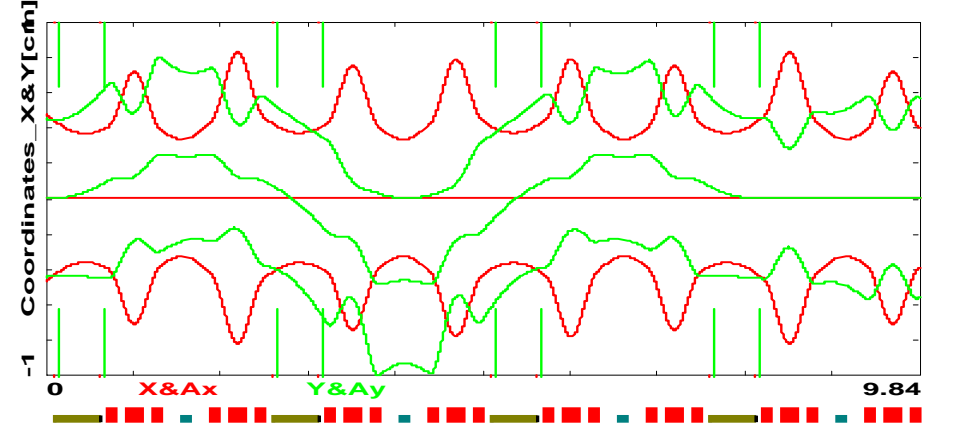
## Effect of RF cavities

- Cav.  $\perp$  focusing destroys the optics periodicity
- For  $f_{RF}=325$  MHz &  $\mu_L=90$  deg
  - ◆ Cavity focusing:  $F=-260$  cm
- RF cavities have to be moved from centers of RF straights to make space for beam dump
- It strongly amplifies  $\beta_x$  beating

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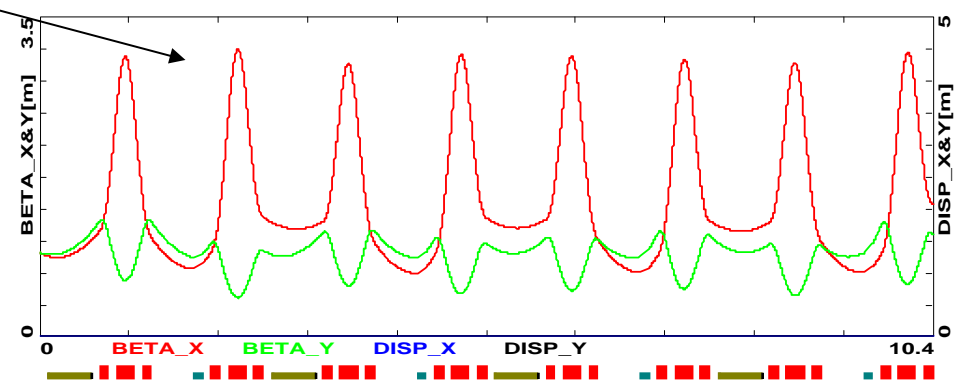


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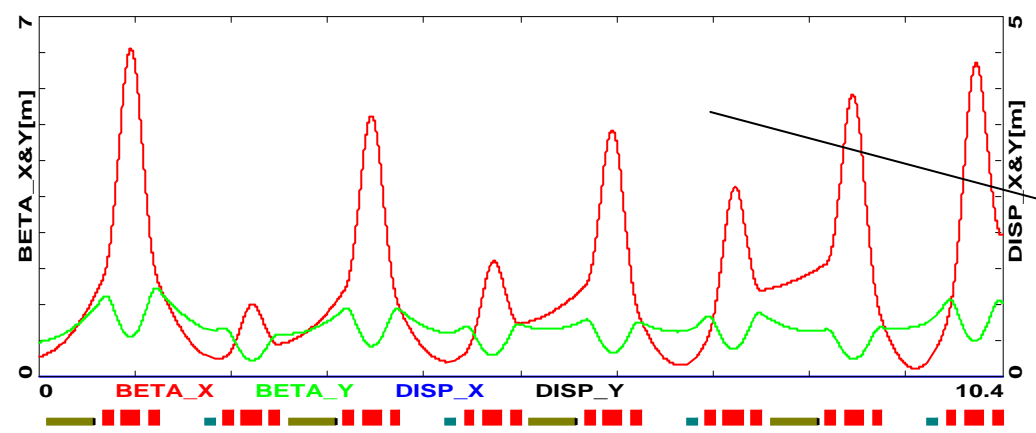
*Symmetr. cav. pos.:  $3\sigma$  beam size in absence of cavity focusing;  $G_F=0.522$  &  $G_D=0.595$  kG/cm  
 $\mu_x=\mu_y=2.01$  V kick  $\pm 170$  V, gap  $\pm 6.33$  mm,*

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*Asymmetric cavity location*

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- Optics correction results in 2 times reduction of  $\beta_{Xmax}$



# MEBT Optics (continue)

- Correction of focusing requires
  - ◆ Vertical
    - Three families of defocusing quads
  - ◆ Horizontal
    - Each focusing quad is regulated independently

## Major parameters of MEBT

Beam energy	2.5 MeV
Beam current	5 mA
Longitudinal rms emittance	1 $\mu\text{eV s}$
Normalized rms $\perp$ emittance	0.2 mm mrad
Norm. emittance ratio: $\varepsilon_L/\varepsilon_\perp$	1.6
Longitudinal phase advance	90 deg (per 2 cells)
Transverse phase advance	$\sim$ 90 deg (per 1 cell)
Bunch (RFQ) frequency	162.5 MHz
RF frequency	325 MHz
RF voltage	41 kV

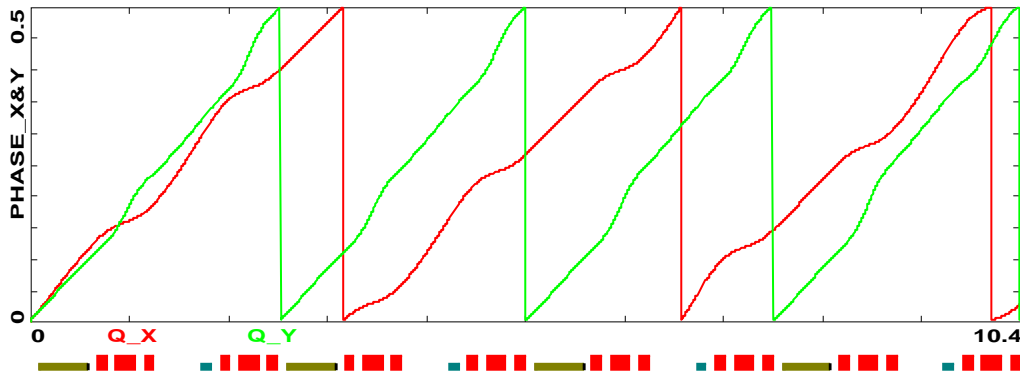
## Quad parameters

Name	L[cm]	G[kG/cm]
qD	10	-0.5308
qF1	20	0.4558
qD1	10	-0.5408
qD2	10	-0.6378
qF2	20	0.4698
qD	10	-0.5308
qD	10	-0.5308
qF3	20	0.4438
qD1	10	-0.5408
qD2	10	-0.6378
qF4	20	0.4718
qD	10	-0.5308
qD	10	-0.5308
qF5	20	0.4438
qD1	10	-0.5408
qD2	10	-0.6378
qF6	20	0.4718
qD	10	-0.5308
qD	10	-0.5308
qF7	20	0.4448
qD1	10	-0.5408
qD2	10	-0.6378
qF8	20	0.4558
qD	10	-0.5308

# MEBT Optics with space charge

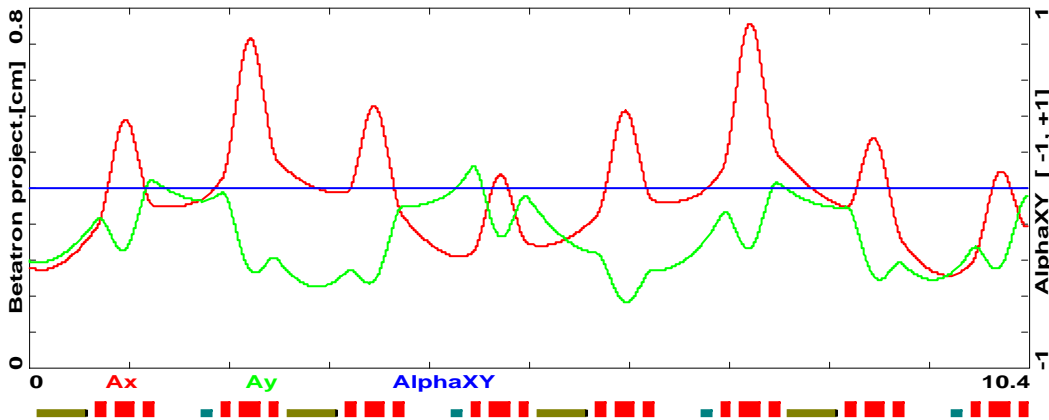
■ Without space charge:  $\mu_x \approx \mu_y \approx 90^\circ$

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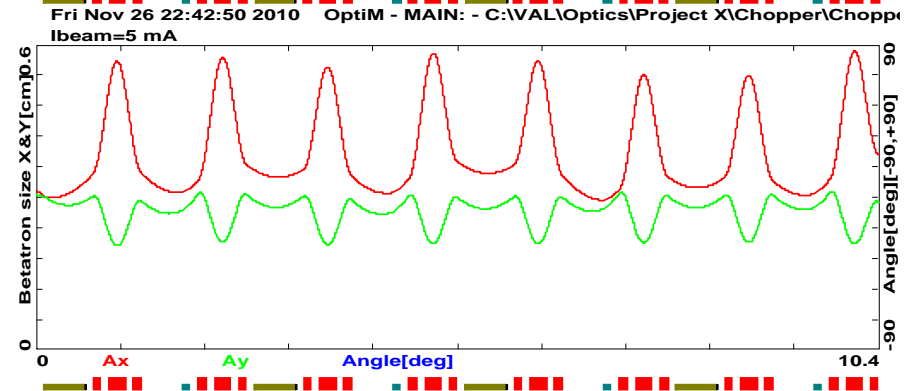
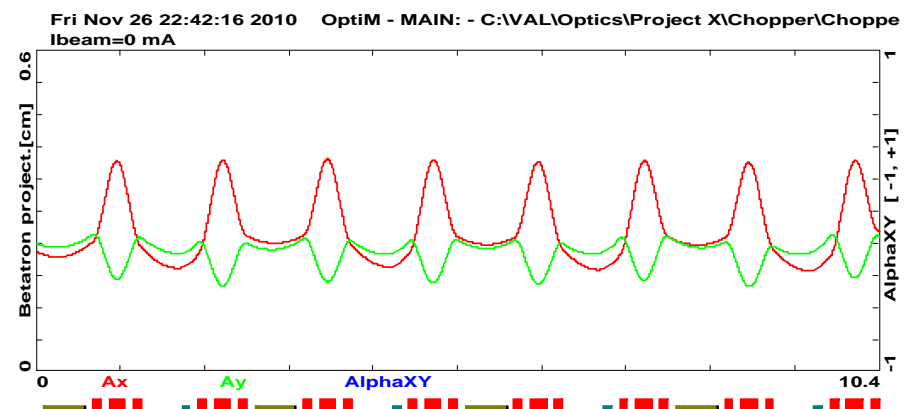


■ If not tuned the space charge yields large beam envelope oscillations

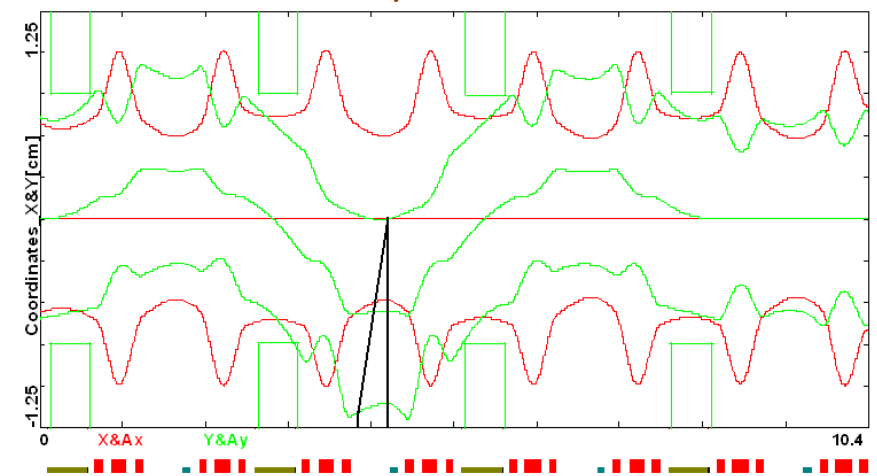
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■ Matching at MEBT entrance strongly suppresses the oscillations



*Beam envelopes  $\sqrt{2}\sigma$  for  
0 mA - top, 5 mA bottom*



*$3\sigma$  beam envelopes; 0 mA scaled to 5 mA  
V kick  $\pm 230$  V, gap  $\pm 7.4$  mm,*

# MEBT Optics (continue)

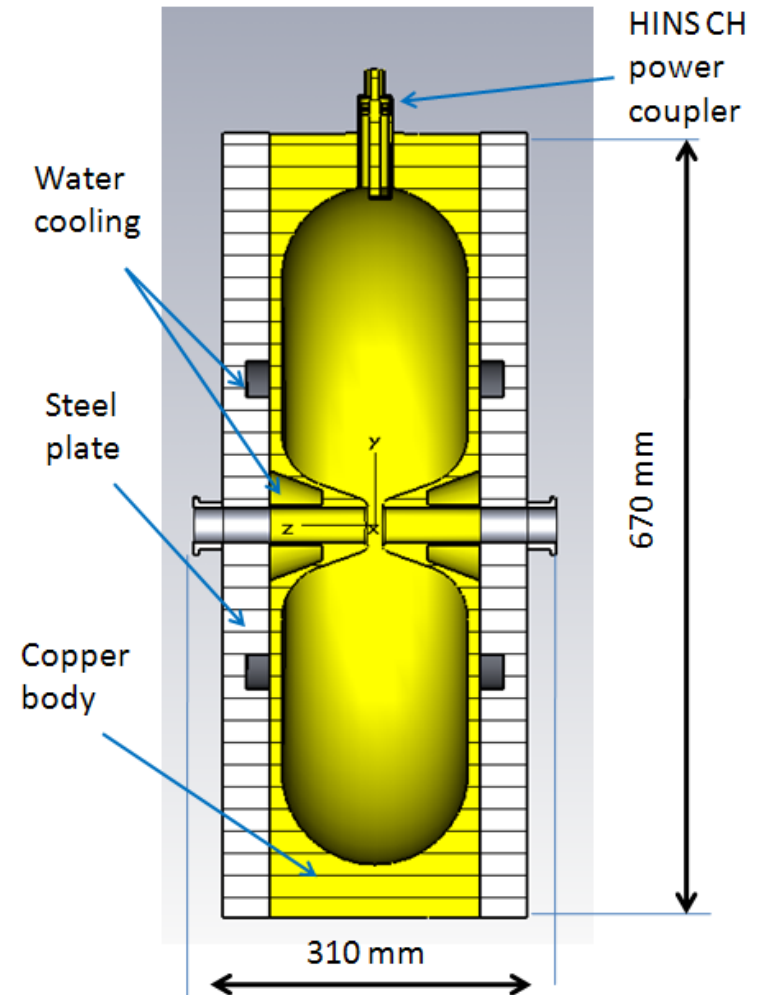
## ■ Period structure

Name	qD	drift	qF	drift	qD	drift
Length [cm]	10	10	20	10	10	70

- ◆ Quads:  $G < 0.7$  kG/cm; aperture:  $\varnothing = 4$  cm,  $B_{\text{tip}} < 1.4$  kG

## ■ RF cavities

- ◆ 325 MHz looks good if the longitudinal emittance  $\leq 1 \mu\text{eV s}$ 
  - $\sigma_{\phi_{\text{max}}} = 18$  deg  
@  $1 \mu\text{eV s}$  &  $I_{\text{beam}}=0$
- ◆ Period 260 cm,  $V=41$  kV,  $\mu_L=90$  deg.
  - Larger emittance will require 162.5 MHz cavities with 2 times larger voltage ( $\sim 82$  kV)
  - For the same  $\mu_L$  the low frequency RF will have the same effect on transverse focusing

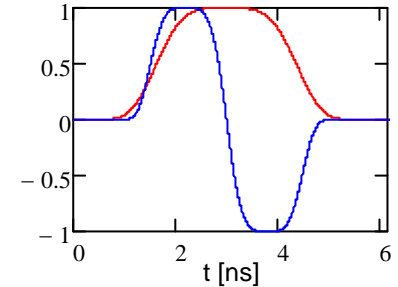


# Summary for MEBT optics

- Kicker requirements:  $L=50$  cm,  $V_{eff}=\pm 250$  V, gap 15 mm
  - ◆ Almost 2 times reduction of kicker voltage is related to
    - Using vertical kick instead of horizontal - 1.25 times
    - Reduction of emittance from 0.4 to 0.2 mm mrad ~1.4 times
  - ◆ Space charge increases the beam size
    - ⇒ required kick grows by 1.35 times from 0 to 5 mA (170 -> 230 V)
- Beam dump - large beam power (up to 12.5 kW)
  - ◆ Allocated space for RF cavity and beam dump is 70 cm
  - ◆ It is tight
    - Can be alleviated by shortening quads => total length of triplets
      - a design is required to see how much can be gained

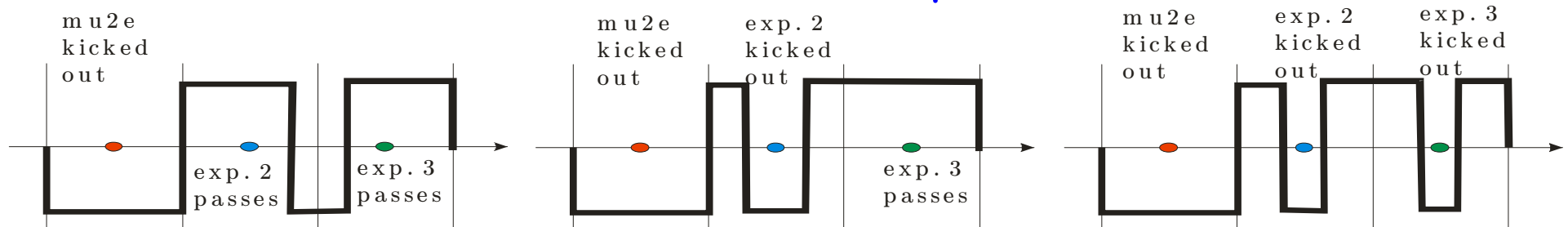
## ■ Bipolar kicks: "+" - no chop; "-" - chop; "0" - half bunch chop

- ◆ It allows the beam current regulation
- ◆ It reduces the voltage of power amplifier by 2 times
- ◆ Allows to use an amplifier without DC coupling but requires twice larger bandwidth
  - Absence of DC coupling => effective protection of kicker overheating by the beam halo with detecting DC current



## ■ Longitudinal tails of RFQ can limit the beam extinction

- ◆ It can be addressed by pulse shape adjustments for one experiment (mu2e) but can be done for all experiments
- ◆ It will be easier for a single polarity (entire bucket) kick
- ◆ Simulations are needed to make a quantitative conclusion





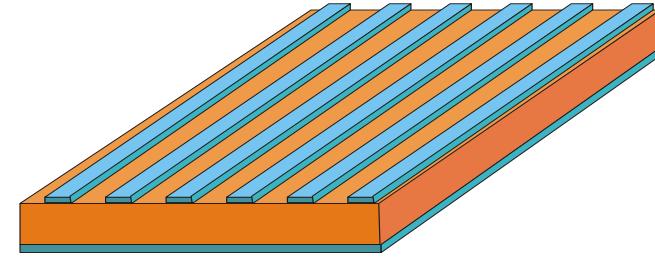
## **Bunch-by-Bunch Kickers**

- 4 kickers:  $L=50$  cm,  $U_{\text{eff}}=\pm 250$  V (gap 15 mm)
- 6.1 ns between bunches
  - ⇒ Bunch-to-bunch distance 13.4 cm
  - ⇒ Bandwidth  $\sim 0.3$  GHz for bipolar kicks
  - ⇒ The pulse velocity should match the beam velocity
- There are 3 ways to decelerate the wave
  - ◆ Spiral (old GHz scopes)
  - ◆ Meander (CERN proposal)
  - ◆ short kickers connected by a coaxial delay lines
- The major reasons limiting the bandwidth are
  - ◆ coupling between stripes
  - ◆ reflections from discontinuities
  - ◆ losses in the conductor and dielectric

## Simple analytical model for signal propagation

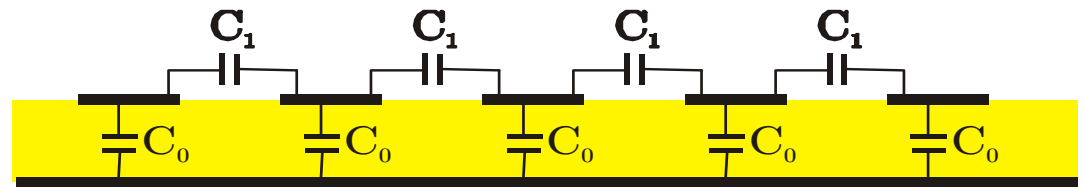
- In the absence of coupling between nearby lines it can be considered as a transmission line

- ◆ Dispersion is small
  - Dominated by loss in the conductor



- Equations for parallel lines (coupling is on)

$$\begin{cases} \frac{\partial I_n}{\partial x} = -C_0 \frac{\partial U_n}{\partial t} + C_1 \left( \frac{\partial U_{n+1}}{\partial t} + \frac{\partial U_{n-1}}{\partial t} \right) \\ \frac{\partial U_n}{\partial x} = -L_0 \frac{\partial I_n}{\partial t} \mp L_1 \left( \frac{\partial I_{n+1}}{\partial t} + \frac{\partial I_{n-1}}{\partial t} \right) \end{cases}$$



sign “-” if currents in nearby lines go in the same direction, “+” - otherwise  
 $C_0$  and  $L_0$  are capacitance and inductance per unit length;  $n$  - numerates lines

- If the same signals are propagated simultaneously in all lines the propagation speed is the same as in a single line

⇒ In the first order of perturbation theory the inductive and capacitive coupling coefficients are

equal  $\kappa = \frac{C_1}{C_0} = \frac{L_1}{L_0}$

## Coupling between stripes

- Capacitance per unit length of a single stripe is (Gelmont, et.al.,1995)

$$C_0 \approx \frac{1+\varepsilon}{2} \begin{cases} \left[ \ln \left( \frac{\sqrt{\cosh(\alpha(b, w, \varepsilon)) + 1}}{\sqrt{\cosh(\alpha(b, w, \varepsilon)) - 1}} \right) \right]^{-1}, & \tanh(\alpha(b, w, \varepsilon)) \leq 1/\sqrt{2}, \\ \frac{1}{\pi^2} \ln \left( 2 \frac{\sqrt{\cosh(\alpha(b, w, \varepsilon)) + \sqrt{\sinh(\alpha(b, w, \varepsilon))}}}{\sqrt{\cosh(\alpha(b, w, \varepsilon)) - \sqrt{\sinh(\alpha(b, w, \varepsilon))}} \right), & \tanh(\alpha(b, w, \varepsilon)) \geq 1/\sqrt{2}, \end{cases}$$

$$\alpha(b, w, \varepsilon) = \frac{\pi w \varepsilon}{4b(1+\varepsilon)}.$$

- for  $w \ll b, h$  it can be simplified

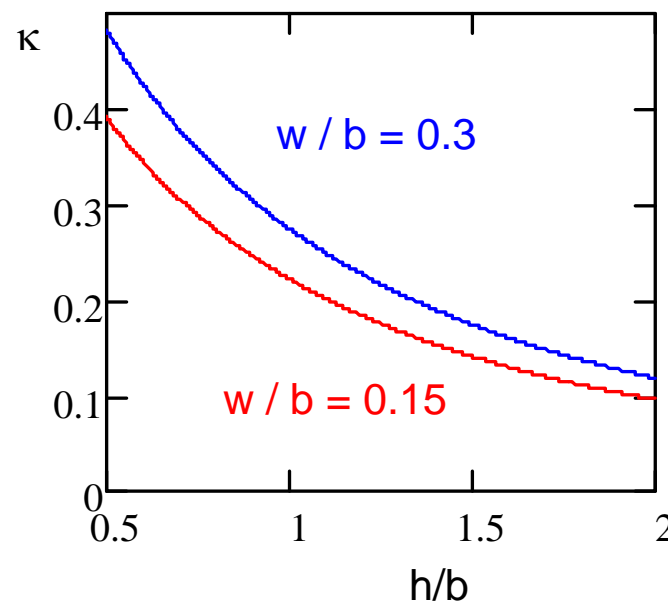
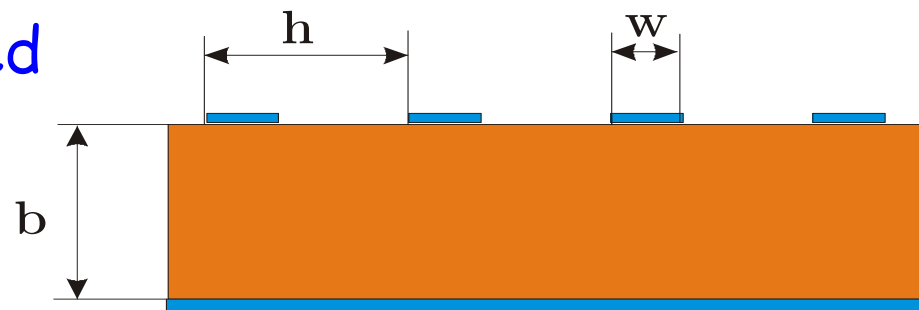
$$C_0 \approx \frac{\varepsilon + 1}{\ln(5.63 b / w)}$$

- Then, the coupling coefficient is

$$\kappa \approx \frac{\ln(1 + (2b/h)^2)}{2 \ln(5.63 b / w)}, \quad w \ll b, h$$

- A desire to have good kicker efficiency ( $U_{\text{eff}} \geq 0.7U_0$ ) requires  $h \leq b$

$$\Rightarrow \kappa \geq 0.15$$



## Coiled kicker

Looking for a

solution in the form:

$$\begin{pmatrix} U(s,t) \\ I(s,t) \end{pmatrix} = \begin{pmatrix} U_0 \\ I_0 \end{pmatrix} e^{i(\omega t - kx)}$$

and taking into account

the boundary condition:

$$\begin{cases} U_{n+1}(s,t) = U_n(s+L,t) \\ I_{n+1}(s,t) = I_n(s+L,t) \end{cases}$$

one obtains the dispersion equation

$$k \approx \sqrt{\varepsilon} \frac{\omega}{c} \left[ 1 + 8\kappa^2 \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \sin^2\left(\sqrt{\varepsilon} \frac{\omega l}{2c}\right) \right]$$

$l$  - length of a single turn

$\varepsilon$  - is dielectric permittivity (assume  $\varepsilon \gg 1$ )

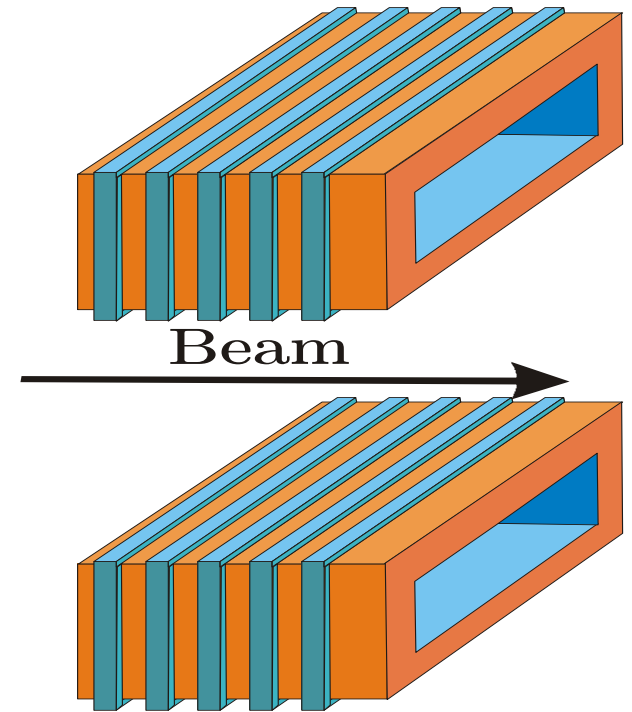
Impedance of the line is frequency dependent too

$$Z(\omega) \approx Z_{line} \left[ 1 + 2\kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right], \quad Z_{line} = Z_0 \frac{\sqrt{\varepsilon}}{4\pi C_0}$$

Reflections modulate the wave amplitude propagating along beam

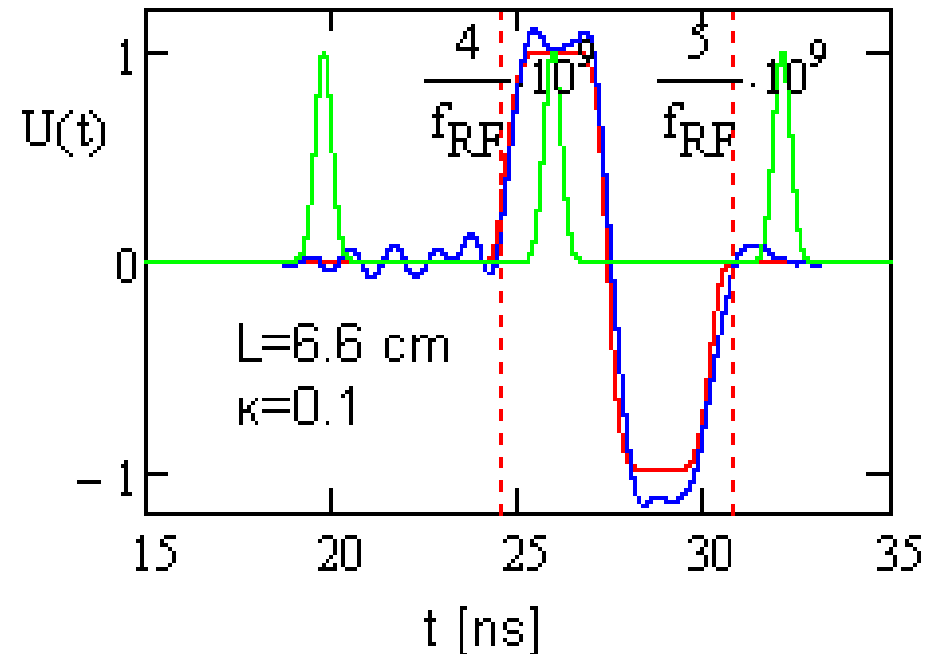
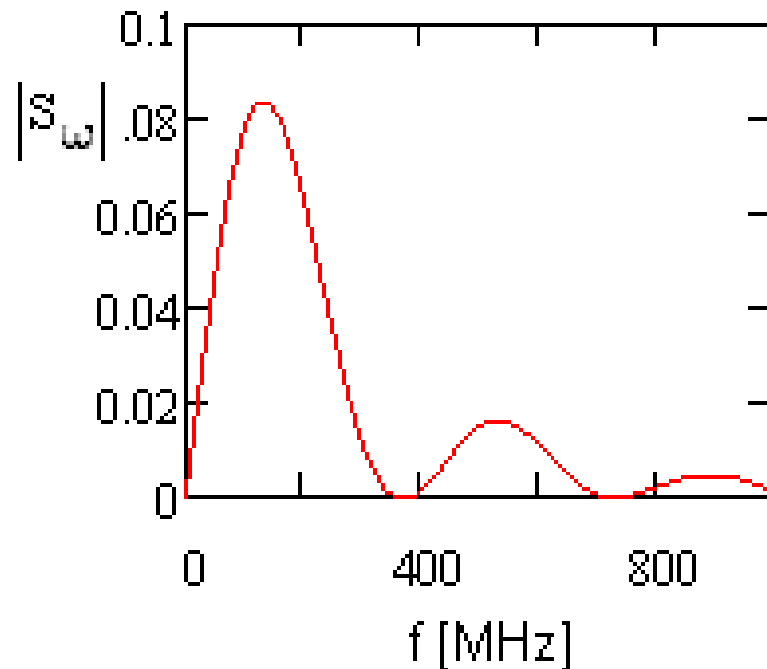
$$U(\omega) \approx U_0 \left[ 1 + \kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right]$$

Wave reflected from termination weakly interacts with beam



## Coiled kicker (continue)

- Phase modulations,  $\exp(-ik(\omega)s)$ , affect the pulse propagation stronger than the wave reflections from the kicker due to frequency dependent mismatch
  - ◆ Damping due to finite resistivity makes only small correction



*turn length -  $l=6.6$  cm,  $\kappa=0.1$ ,  $\epsilon=3.5$ ,  $h=9$  mm, total length - 50 cm*

- Coupling coefficient was set to obtain sufficiently small pulse distortions
  - ◆  $\kappa \leq 0.1 \Rightarrow$  large distance between turns  $\Rightarrow$  large kick attenuation
    - Reduction of one turn length would help but is limited by kicker width (i.e. beam size)
  - ◆ Therefore the coiled kicker does not look promising

## Meander kicker

Looking for solution in the form:

$$\begin{pmatrix} U(s,t) \\ I(s,t) \end{pmatrix} = \begin{pmatrix} U_1 e^{-ik_n x} + U_2 e^{ik_n x} \\ I_1 e^{-ik_n x} + I_2 e^{ik_n x} \end{pmatrix} e^{i(\omega t - mn)}, \quad k_n = \begin{cases} |k|, & \text{odd } n \\ -|k|, & \text{even } n \end{cases}$$

and taking into account the boundary condition:

$$\begin{cases} U_n(l/2, t) = U_{n+1}(l/2, t) \\ I_n(l/2, t) = I_{n+1}(l/2, t) \end{cases}$$

one obtains the dispersion equation

$$\mu(\omega) \approx \sqrt{\varepsilon} \frac{\omega l}{c} - \kappa \sin\left(2\sqrt{\varepsilon} \frac{\omega l}{c}\right)$$

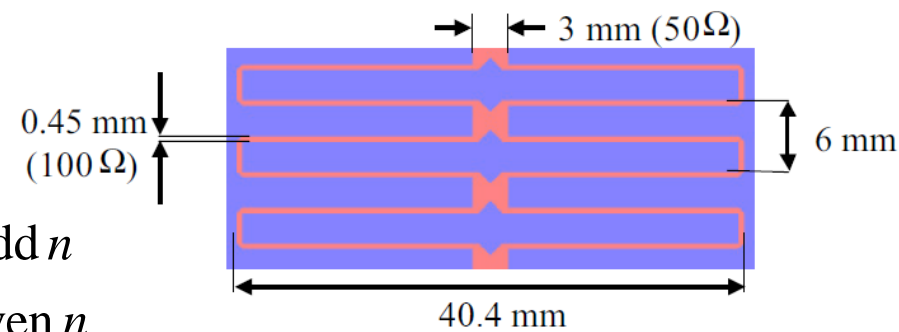
$l$  - length of a stripe (kicker half width)

$\varepsilon$  - is dielectric permittivity (assume  $\varepsilon \gg 1$ )

In the first order the line impedance and wave reflections are the same as for coiled kicker

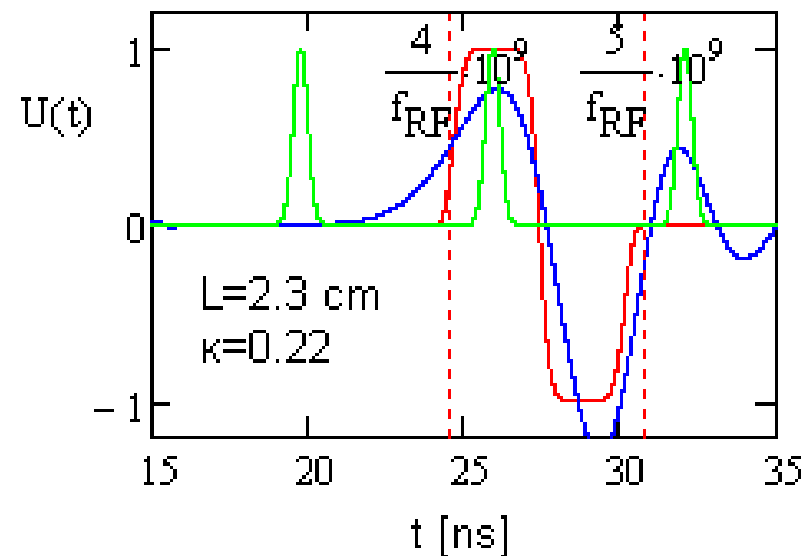
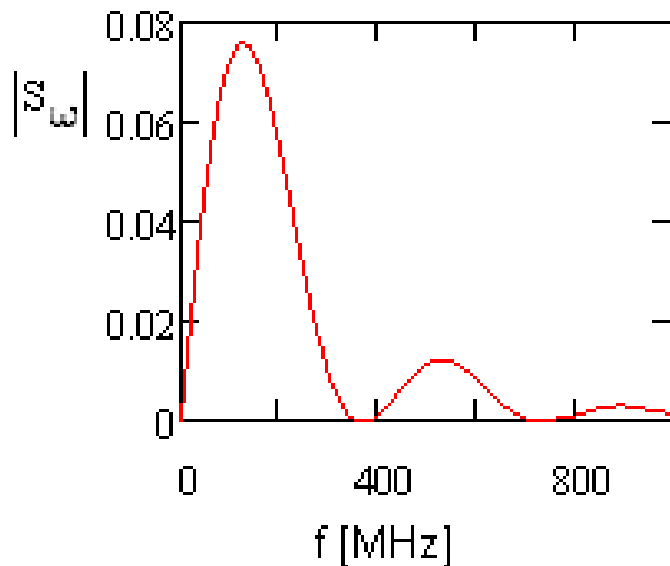
$$Z(\omega) \approx Z_{line} \left[ 1 + 2\kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right], \quad Z_{line} = Z_0 \frac{\sqrt{\varepsilon}}{4\pi C_0}$$

$$U(\omega) \approx U_0 \left[ 1 + \kappa \cos\left(\sqrt{\varepsilon} \frac{\omega l}{c}\right) \right]$$



## Meander kicker (continue)

- The same as for coiled kicker the wave reflected from termination weakly interacts with beam
- Not as for coil kicker the dispersion correction is  $\propto \kappa$ , not to  $\kappa^2$ 
  - ◆ i.e. much larger effect for the same coupling
- However much shorter period (more than 4 times) helps
  - ◆ It moves problems to higher frequencies
- Still looks that it does not address Project X needs



*Pulse spectrum and propagation for the CERN kicker proposal adjusted to project X needs,  
 $L_{tot}=50$  cm,  $h = b = 3$  mm,  $l = 22$  mm,  $\varepsilon = 9.6$*

# CERN proposal for meander kicker

## ■ Total kicker length 40 cm

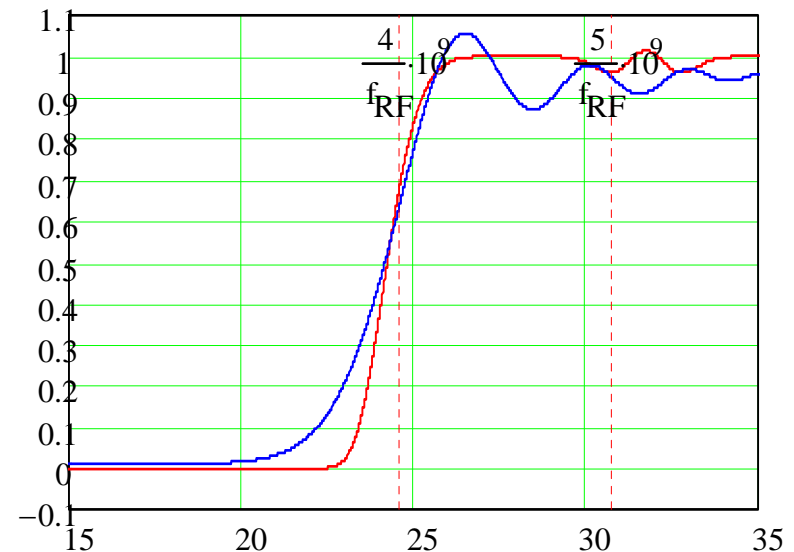
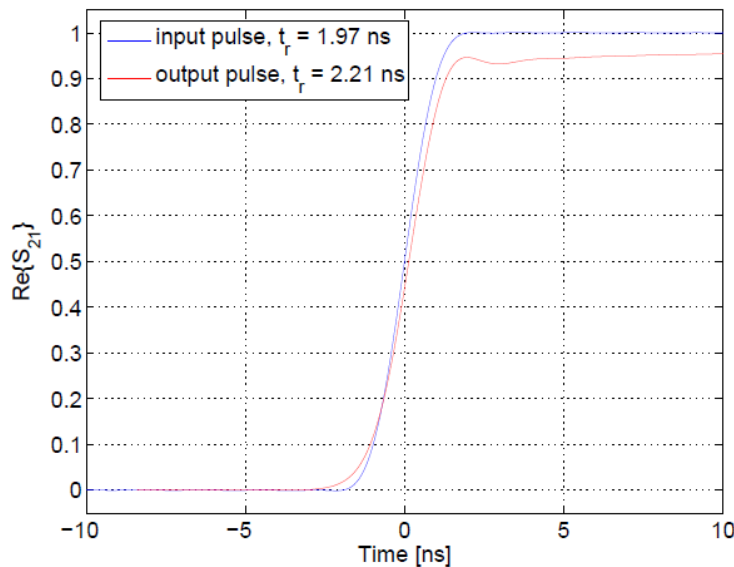
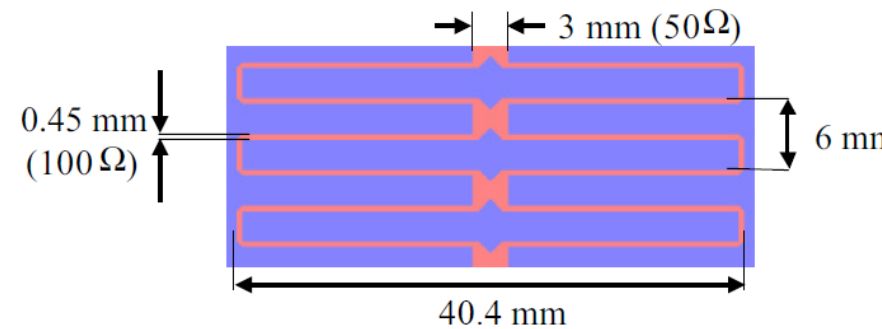
- ◆ two 100  $\Omega$  lines

## ■ Demonstrated rise time $\sim 3$ ns

- ◆ They claim 1 ns (definition?)

## ■ The above analytical estimate looks less optimistic ( $\sim 5$ ns)

- ◆ It correctly predicts that the wave propagates faster by 1.9 times because of strip-to-strip coupling
  - $\kappa = 0.22$  - analytical estimate
  - $\kappa = 0.25$  - fitted from wave propagation speed



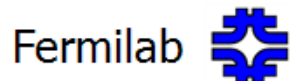
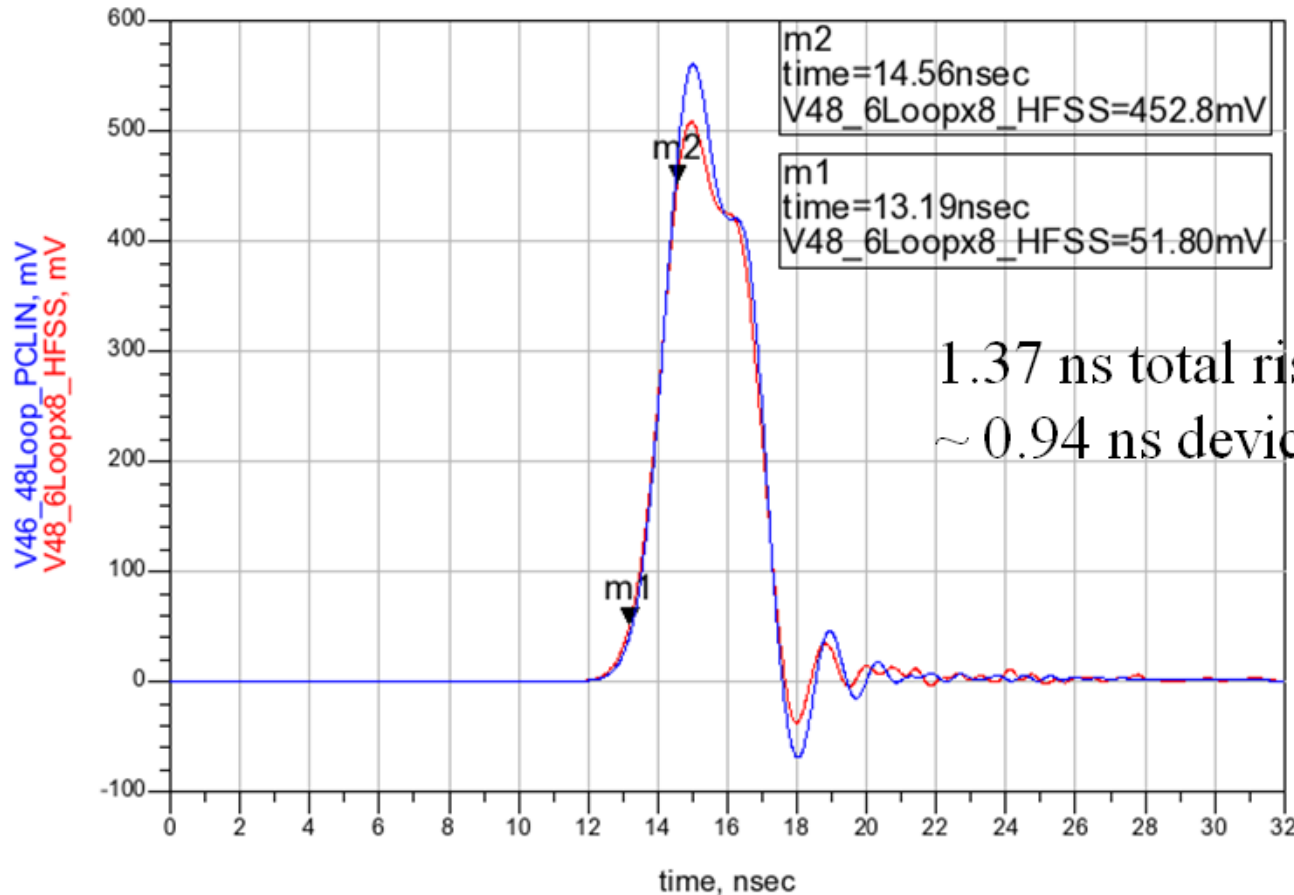
*Measured and calculated wave shape at the kicker end*



# CERN proposal for meander kicker (continue)

## ADS/HFSS 48 CERN Loops

48 Loops (Double Meander), 4 ns pulse



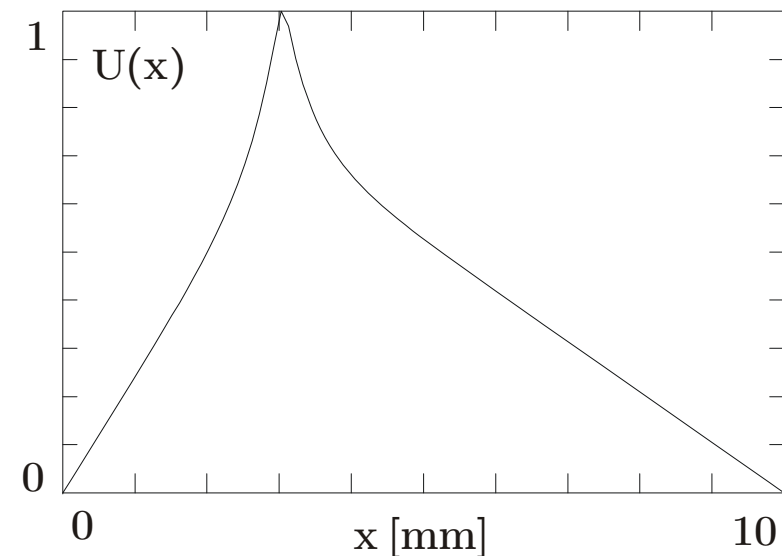
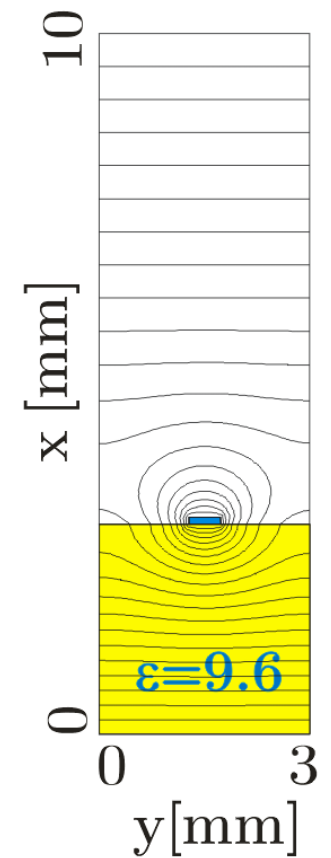
Ding Sun - Project X Meeting

May 4, 2010

*Total length of 48 loops is 28.8 cm; single polarity pulse fits into 6 ns*

## Complications with CERN meander kicker proposal

- Hardly can achieve the desired bandwidth (time resolution)
- Bad kicker efficiency:  $\sim 60\%$  ( $U_{\text{eff}} \geq 0.6U_0$ )
  - ◆ Large  $\varepsilon$  and  $\rho = 100 \Omega$ 
    - $\Rightarrow$  small stripe width
    - $\Rightarrow$   $\sim 30\%$  loss of the kick due to small width
  - ◆ Additional 15% are lost due to stripe resistivity
    - wave damping  $\sim 30\%$  to the line end (40 cm)
    - corresponding heating is negligible,  $\Delta T \approx 1.5 \text{ C}^\circ$
- Dielectric is directly visible to the beam and can be charged by its tails
  - ◆ Reproducibility???
  - ◆ Discharges can result in a kicker damage



# Alternative Approach for Chopper Design (Ding Sun)

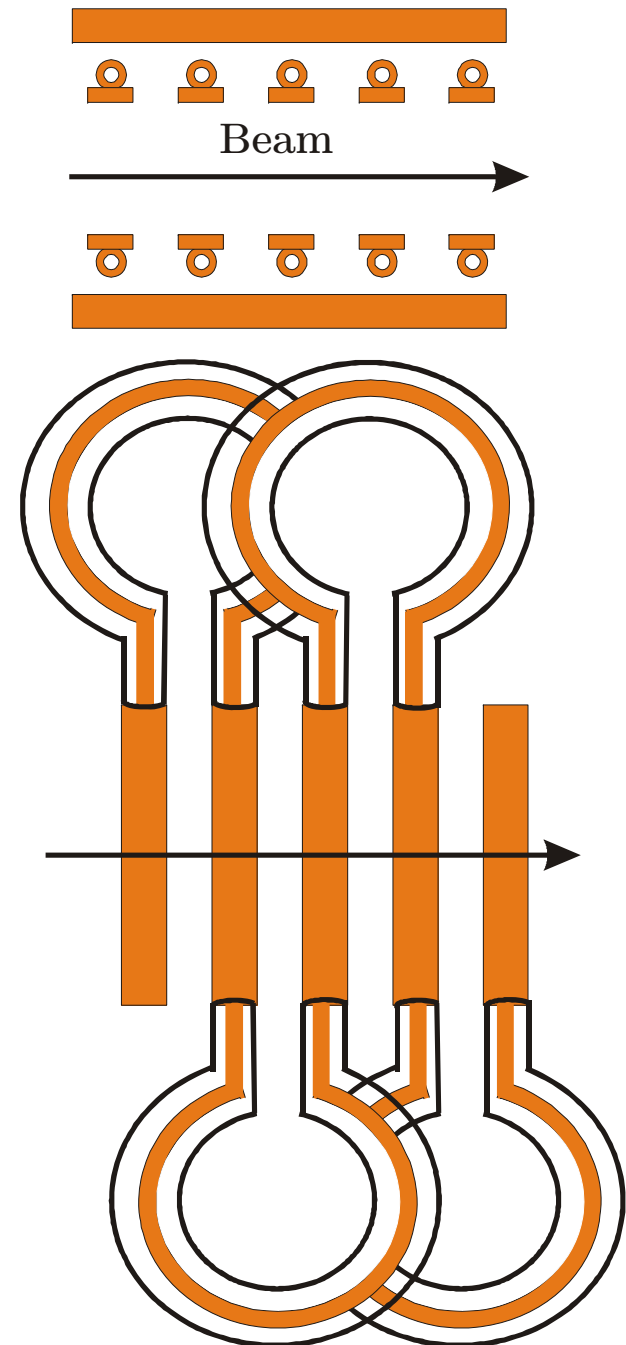
## ■ Details

- ◆ No dielectric
  - No charging of the surface
- ◆ "RF cable" connection between stripes
- ◆ Smaller effective coupling between lines
- ◆ More effective kicks
- ◆ Water or air cooling of stripes is possible

## ■ Expected problems

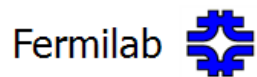
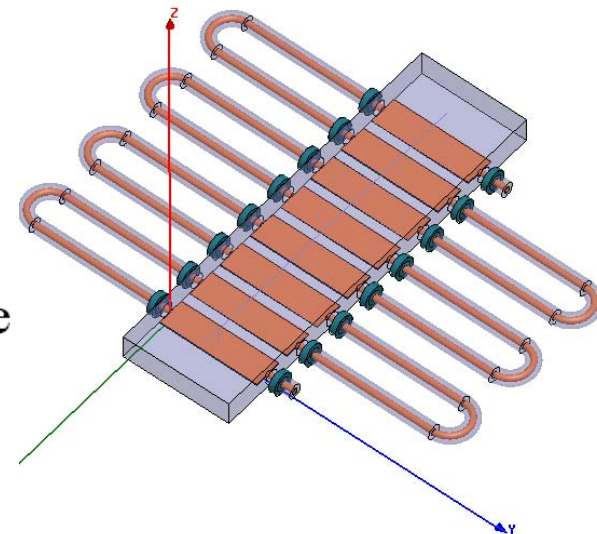
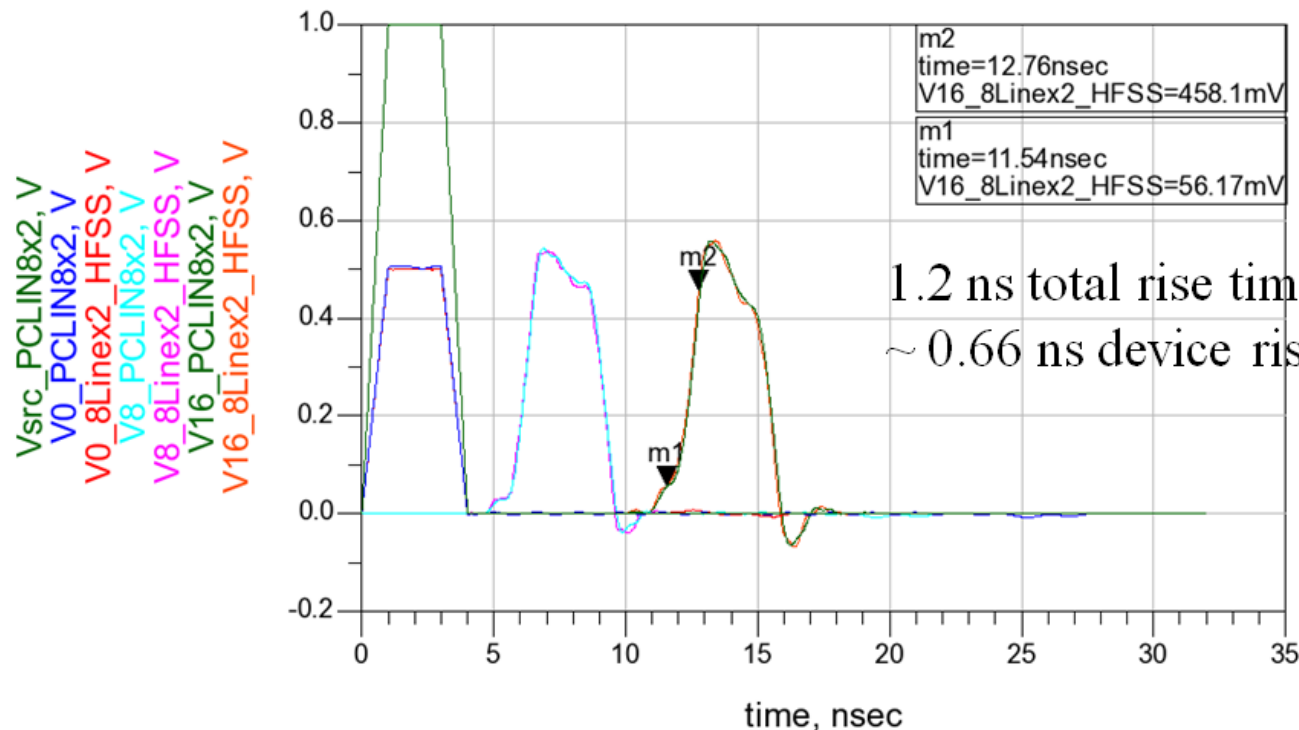
- ◆ Reflections at the transitions

## ■ Construction of prototype based on the cable delays is started



# Alternative Approach for Chopper Design (continue)

16 Striplines, 4 ns pulse / 1 ns rise time



Ding Sun - Project X Meeting

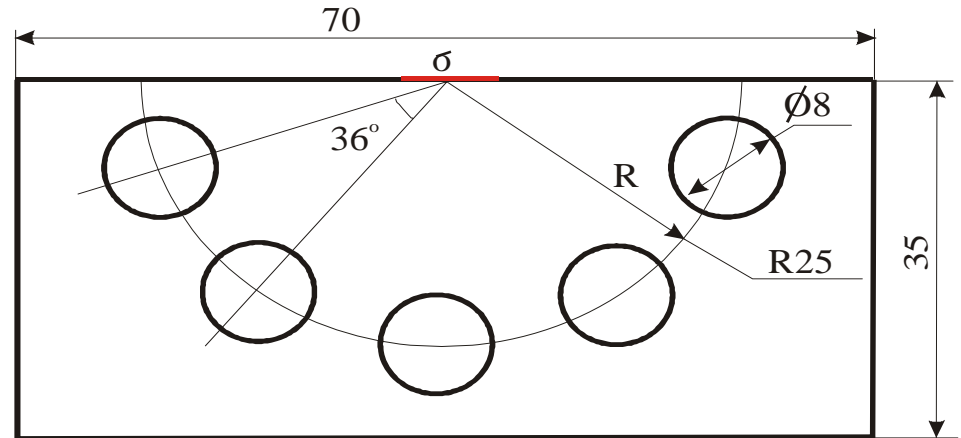
May 4, 2010

*Step - 16 mm, total length for the 16 strip-lines kicker is 26 cm, 2 kickers in 1 straight*

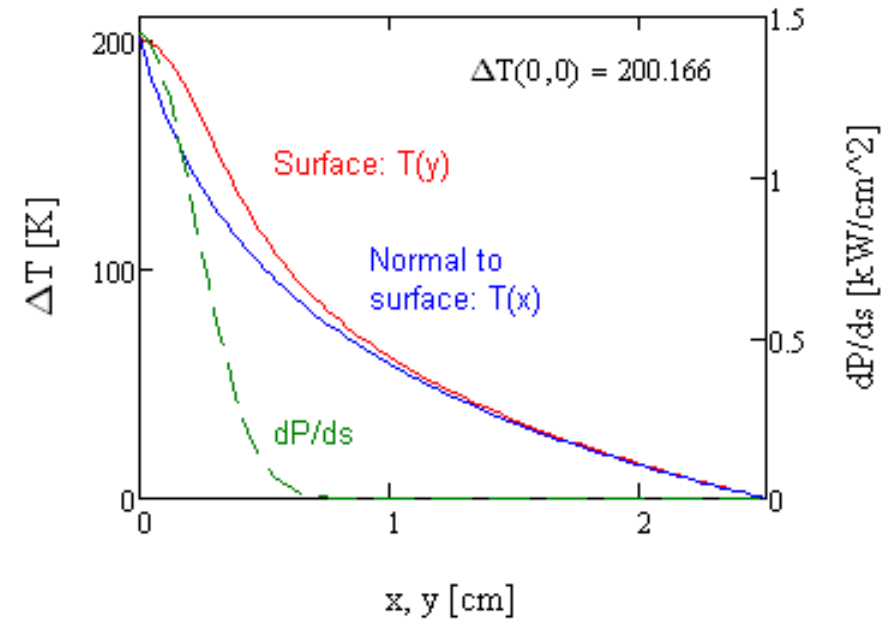
- Rise time is at the boundary of acceptable for double polarity pulse
- Kicker efficiency is much better than for CERN meander
  - ◆ 300 V peak (1 kW) amplifier look adequate for powering one side of the kicker (required effective kicker voltage  $\pm 230$  V)
- First tests are expected within 2 months

# Beam Dump

- For 5 mA beam the total beam power is 12.5 kW
- Water can accept the power density  $dP/ds \leq 60 \text{ W/cm}^2$ 
  - ◆ Heat removal requires large area of water channels
- Temperature gradient in damp material introduces stresses and should be minimized
- For Gaussian heating profile with  $\sigma = 2.2 \text{ mm}$  and the linear power density  $dQ/dL=800 \text{ W/cm}$  the temperature difference in copper  $\sim 200 \text{ K}$  ( $R=2.5 \text{ cm}$ )



$$\Delta T \simeq \frac{1}{\pi \kappa} \frac{dQ}{dL} \ln \frac{1.89R}{\sigma}$$



## Beam dump (continue)

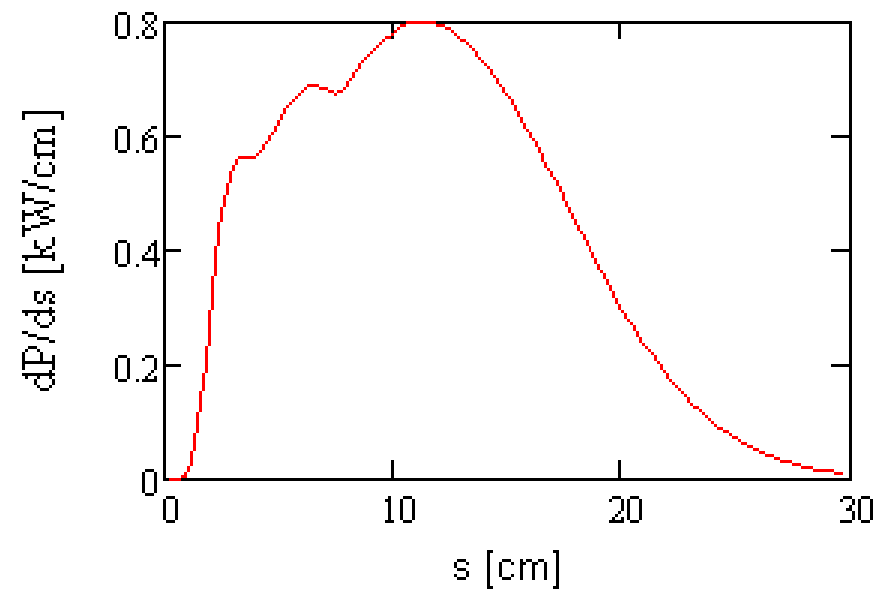
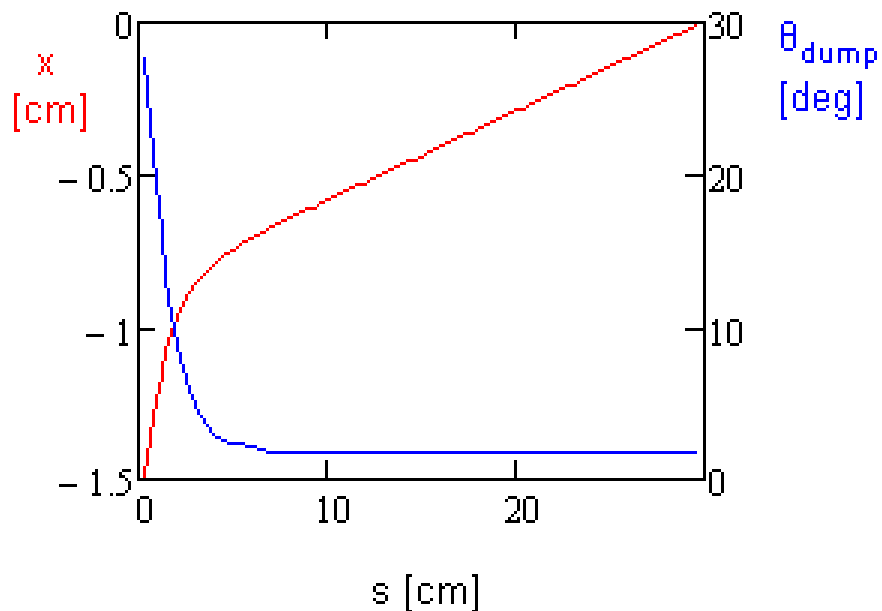
- Copper looks as a good material due to its high thermal conductivity
- However the temperature difference of 200 K results large stresses
  - ◆  $\Delta T = 40$  K @ stress yield
  - ◆ i.e. we are factor of 5 above stress yield
- The stress can be relieved by deformations

- ◆ Half of the stress is absorbed by settling material to mean temperature
- ◆ No significant pulse load
  - $\Delta T = 30$  K for 5 ms interruption
  - Heat penetration (diffusion) rate  $\sqrt{dx^2 / dt} \approx 1$  cm/ $\sqrt{s}$
- ◆ Mechanical design should be done to minimize stresses due to dump heating

Length of the beam dump	30 cm
Beam dump angle to beam	29 mrad
Max. linear power density	<b>0.8kW/cm</b>
Water pressure drop	2 atm.
Water pipes connection	serial
Total length of pipes	2 m
Water flow	0.3 l/s
Power density (water-to-Cu)	64 W/cm <sup>2</sup>
Water $\Delta T$ (inlet-to-outlet)	9.5 C°
$\Delta T$ (water-to-Cu)	27 C°
Inlet water temperature	50 C°
Peak temperature	<b>290C°</b>

## Beam Dump Space Limitations

- 700 mm drift is allocated for the RF cavity and the beam dump
  - ◆ 300 mm cavity
    - ◆ 300 mm beam dump
      - $3\sigma$  scraping
      - Dump face is bend at the entrance to reduce the dump length
    - ◆ 100 mm interfaces



## Beam Dump Lifetime

- Proton ( $H^-$ ) beam destroys the dump surface
  - ◆ Sputtering
    - amplified by oblique incidence - estimate:  $\sim 0.15$  mm/year
  - ◆ Blistering
    - Will be mitigated by high temperature of the dump face  
remelting of blistered material - Dump face should look up
- Dump activation and neutron production
  - ◆ Not negligible
    - Would not happen for Cu at  $E < 2.1$  MeV or with higher Z material
  - ◆ Sputtering limits usefulness of thin layer of high Z material
  - ◆ Thermal stresses do not allow thick layer
- High speed vacuum pumping is required to keep vacuum in MEBT cavities
- Differential pumping is required to keep good vacuum in SC cavities
- Insulators in dump vicinity have to be protected from the flux of spattered material



## Spattering estimate

- The beam energy is sufficiently high and small scattering angle approximation can be used
- Using Thomas-Fermi model for calculating the energy transfer to an atom above  $I_a$  one obtains the cross section:

$$\sigma \approx \pi r_p^2 Z^2 \frac{(m_p c^2)^2}{I_a E} \left( 1 + 0.9 \left( 1.174 \frac{Z^{4/3} r_p}{a_0} \frac{m_p c^2}{\sqrt{4AI_a E}} \right)^{2/3} \right)^{-2}$$

⇒ Spattering probability per incoming proton -  $W \approx \frac{\sigma^2}{a_{lat}^2 \theta}$

$r_p \approx 1.53 \cdot 10^{-16}$  cm,  $a_0 \approx 0.53 \cdot 10^{-8}$  cm,  $m_p c^2 = 938$  MeV,  $E = 2.5$  MeV;

for Cu:  $Z = 29$ ;  $A = 65.5$ ;  $I_a = 3.3$  eV;  $a_{lat} \approx 2.3 \cdot 10^{-8}$  cm (atom-to-atom dist.)

⇒  $W = 5.3 \cdot 10^{-3}$  for  $\theta = 29$  mrad (1.7 deg)

- There is no reliable exper. data on spattering by 2.5 MeV prot.
  - ◆ Comparison to simulations points out ~2 times overestimate
  - ◆ for  $\theta = 1$  deg.: modeling by T. Sizyuk (Perdue univ.) -  $W = 4.3 \cdot 10^{-3}$   
above estimate -  $W = 8.8 \cdot 10^{-3}$
- Applicability condition: incident angle is larger than the scattering angle:  $\theta \gg \sqrt{I/E}$  ( $\theta \gg 1$  mrad)

# Conclusions

- Now we better understand requirements to the RFQ beam parameters (emittances, beam current)
  - ◆ RFQ design and simulations will follow
  - ◆ 10 mA RFQ current greatly complicates the beam bump design
    - Looks impossible without liquid metal jet (reliability?) or significant MEBT lengthening with consecutive negative effect on the beam dynamics
- Reduction of transverse emittance and better understanding of optics reduced the kicker voltage to a manageable level,  $P \leq 1$  kW
- Present understanding of bunch-by-bunch kickers does not support 352 MHz RFQ (162.5 looks OK)
  - ◆ The choice of the kicker type is not quite clear yet