

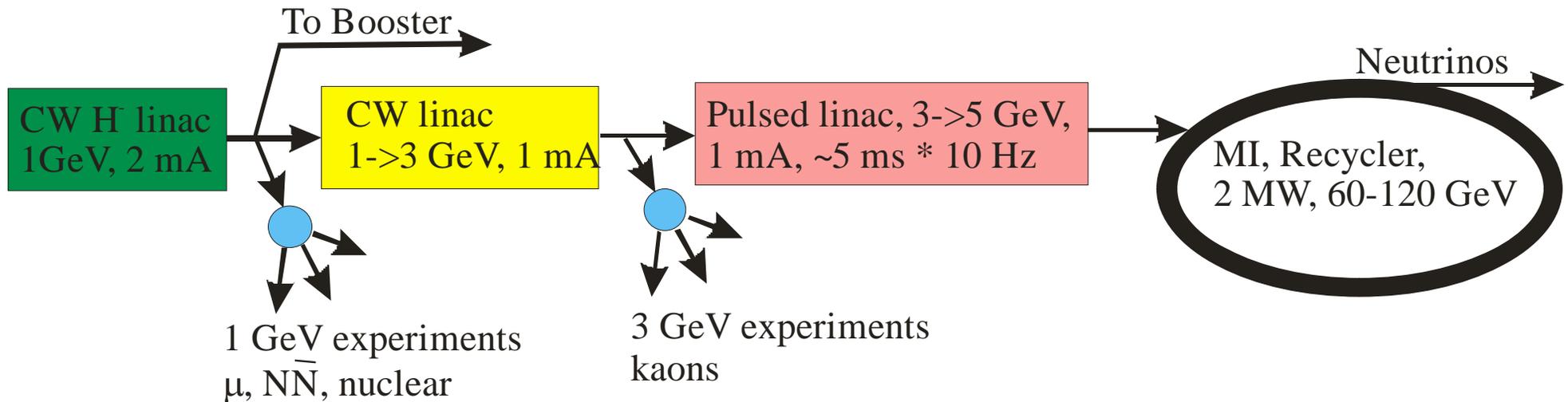
# Acceleration of Muons with Project X Linac

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Mini-Workshop on Muon  
Collider Higgs Factory  
Fermilab  
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# Project X & Project X SRF Technology

- Present plan - Project X to be constructed in 3 stages
  - ◆ Stage 1 -H<sup>-</sup> (a) CW linac, 1 GeV, 1 mA (2 mA?), 162.5→325→650 MHz  
(b) Beam to Booster, 15→20 Hz rep. rate;  $(4.5\rightarrow 6)10^{12}$ /pulse
  - ◆ Stage 2 - (a) H<sup>-</sup> CW linac, 1→3 GeV, 1 mA, 650 MHz;  
(b) 1 mA→2 mA for 1 GeV linac
  - ◆ Stage 3 - (a) Pulsed linac, 1 mA, ~5 ms × 10 Hz(?)  
(b) MI upgrade from 0.7 MW to 2 MW

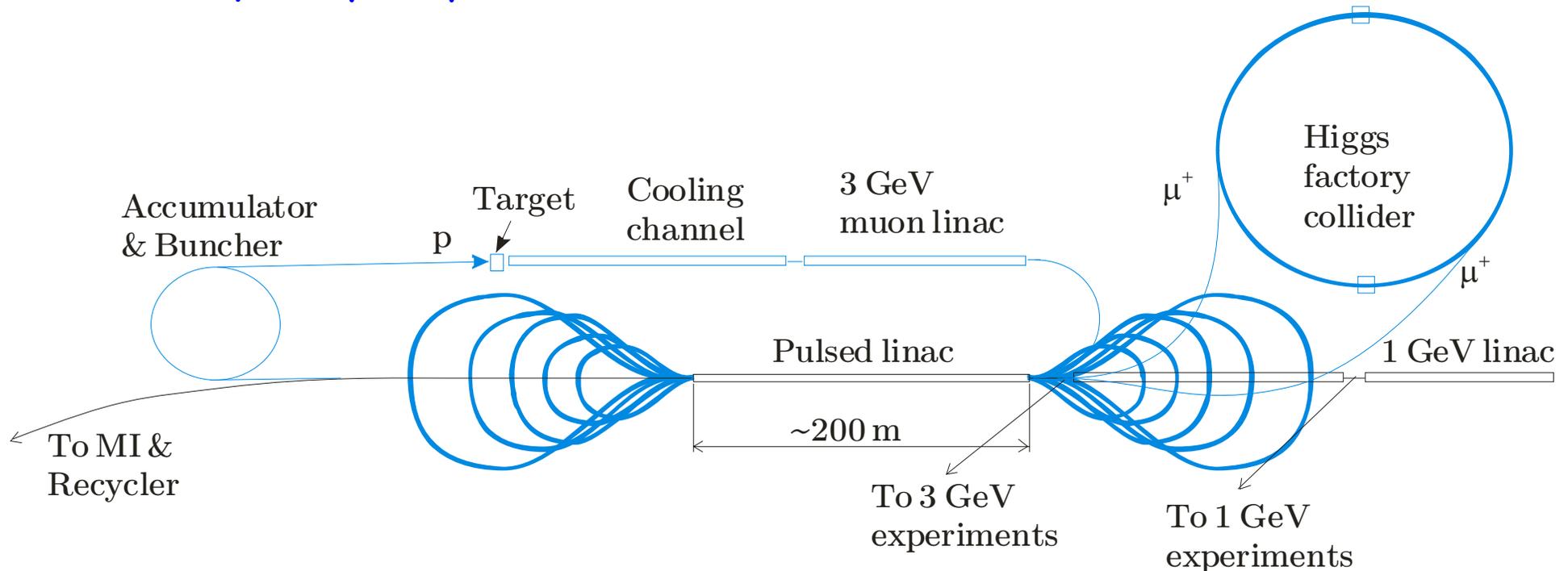


# Project X Pulsed linac (3 -> 8 GeV, 5 GeV installed V)

- Present plan for muon collider pulsed linac
  - ◆ Future upgrade implies
    - Beam current increase from 1 to 5 mA
      - ⇒ will require upgrade of CW part to 5 mA too
    - Beam power increase from 0.34 to 4 MW
      - ⇒ 10 Hz → 15 Hz (?)
      - ⇒ 4.2 ms → 6.7 ms (?)
  - ◆ Pulsed linac upgrade does not imply that it will be used for acceleration of muons
- Possible modification of the plan
  - ◆ 1.3 GHz → 650 MHz
    - ⇒ Acceleration of muons in the Project X pulsed linac
      - Modest (if any) increase in the price for Project X
      - Very significant savings for muon based Higgs factory or  $\nu$ -factory
  - ◆ Cavities are spaced by integer number of cell lengths to allow acceleration into both directions
  - ◆ The Project X and the Project X technology are well aligned with Higgs factory needs

## Details of Modified Plan

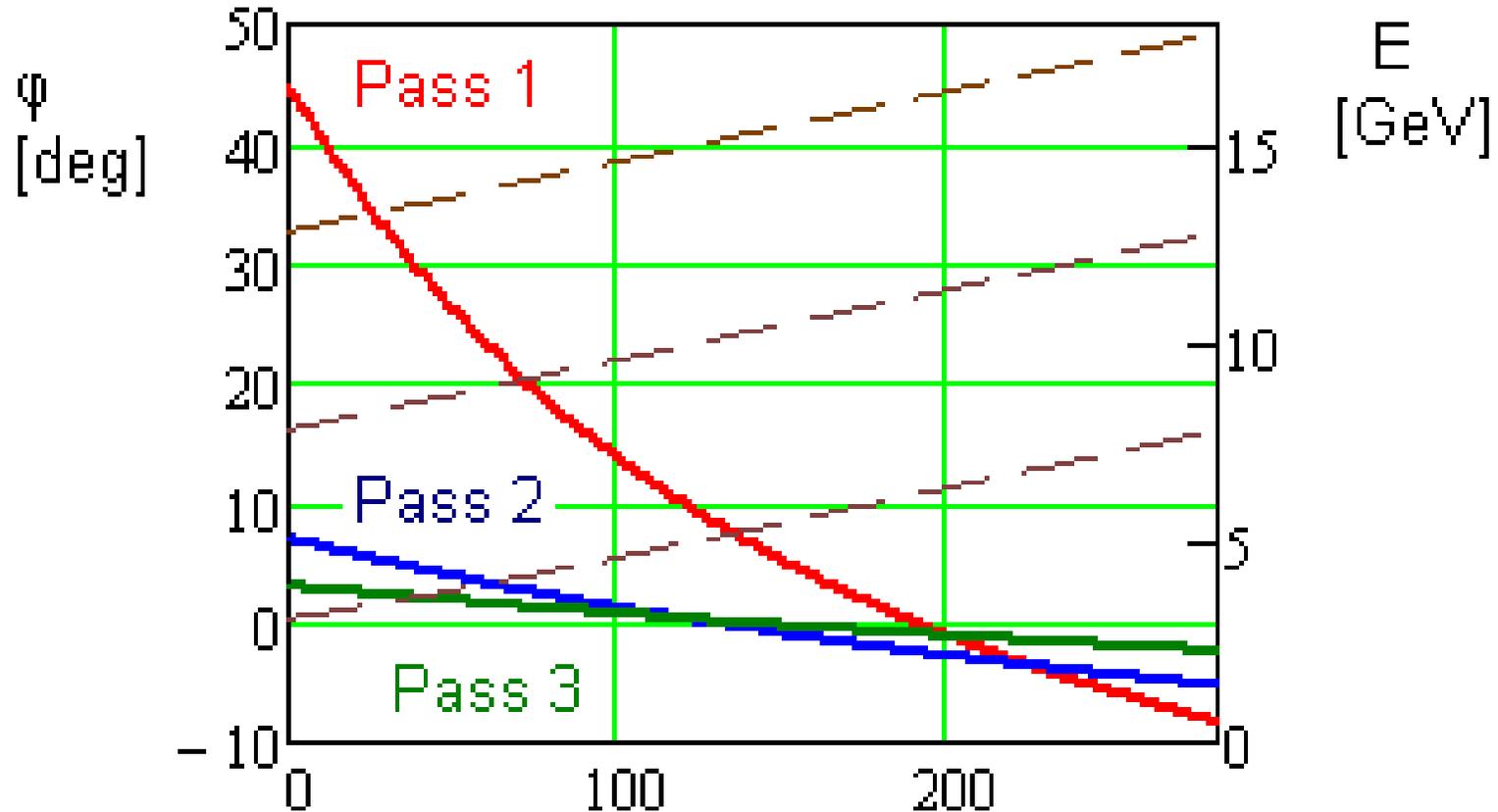
- 12 pass recirculator accelerates muons from 3.1 GeV to 62.5 GeV
  - ◆ s-channel muon based Higgs factory
- Beam power on the muon production target is reduced: 4 → ~1 MW
  - ◆ Beam current stays the same (1 mA)
  - ◆ No need to modify CW part
- RF frequency of pulsed linac decreased from 1.3 GHz to 650 MHz



*Schematic of the Project X and Higgs factory (shown by blue)*

# Initial energy of Recirculation

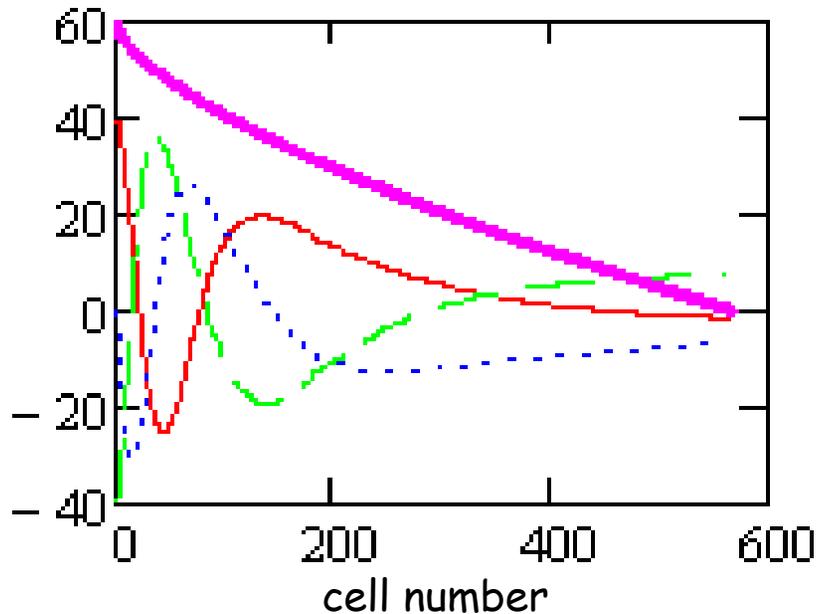
- Phase slip limits the initial energy of recirculation to  $\sim 3.1$  GeV



Phase slip for the first 3 of 12 passes

# Acceleration in the Muon Linac

Long. motion in linac



## Main parameters

Momentum range, pc = [0.3-3.2 GeV]

Accelerating frequency = 650 MHz

Accelerating gradient = 25 MeV/m

Accelerating cavities: 5 cell,  $\beta = 1$

Linac length  $\approx 250$  m

Longitudinal acceptance,  $\varepsilon_{ns} = 3^2 \times 1500$  mm mrad

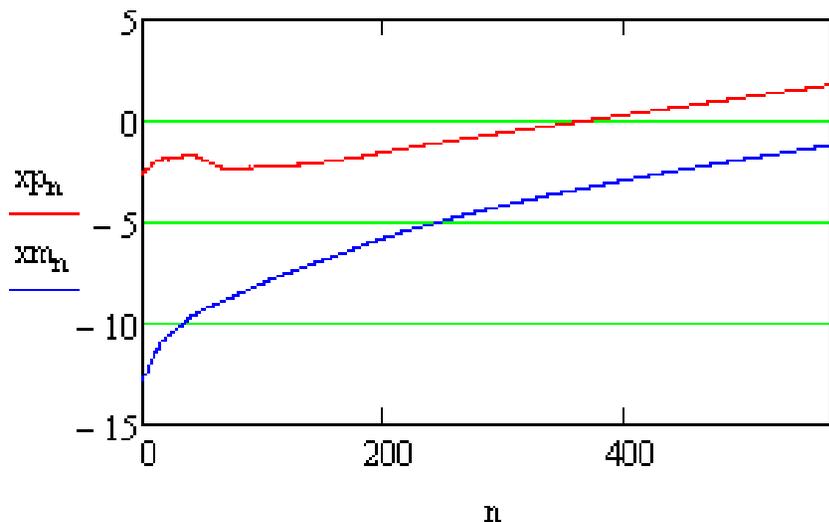
Transverse acceptance,  $\varepsilon_{ns} = 3^2 \times 300$  mm mrad

Number of RF cavities = 114

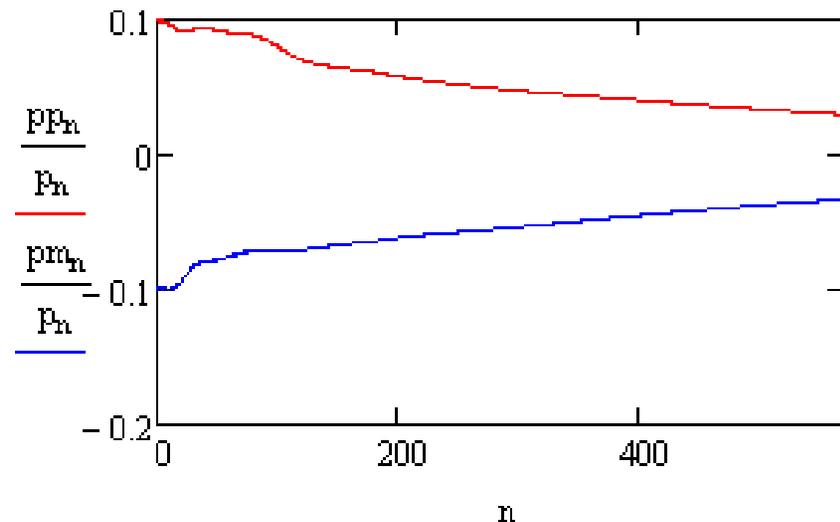
Particles per bunch =  $6 \cdot 10^{11}$

Repetition rate = 10 Hz

Bunch end positions [cm]



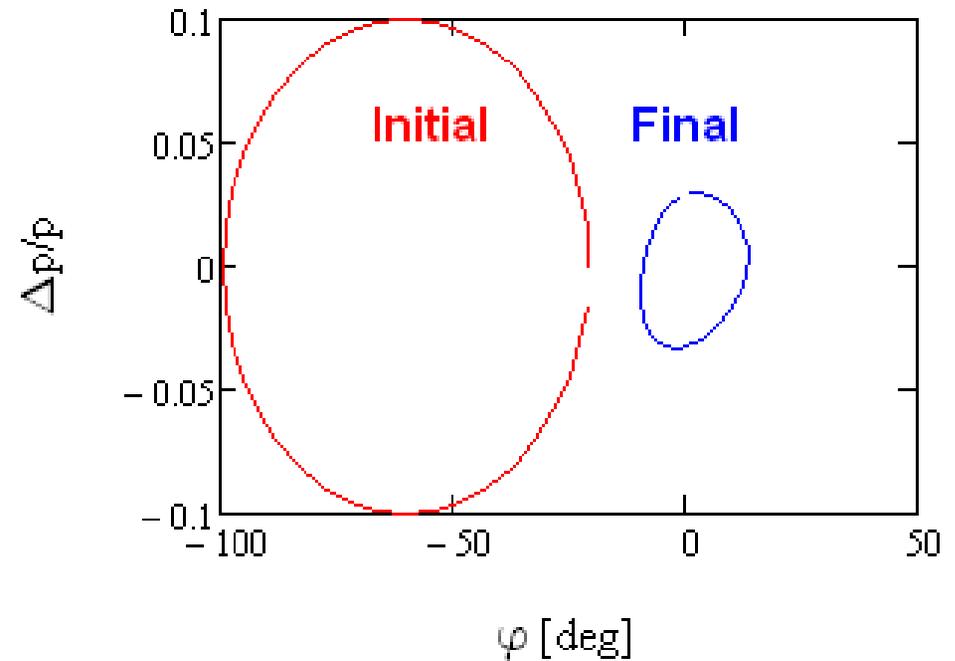
Min. & max. rel. momentum



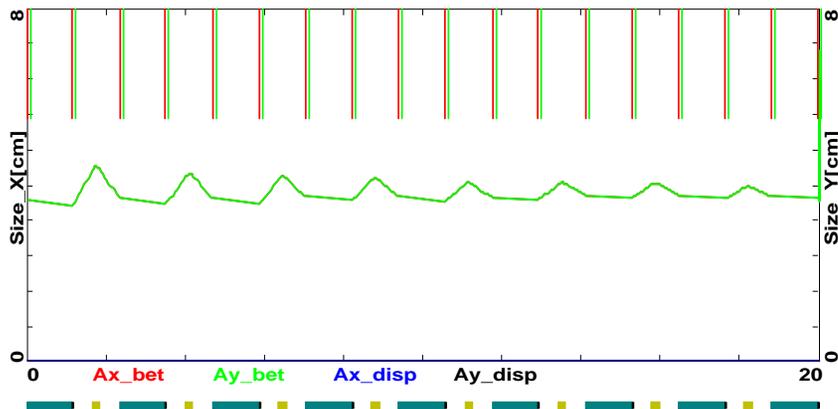
*Bunch boundaries for  $3\sigma$*

# Acceleration in the Muon Linac (continue)

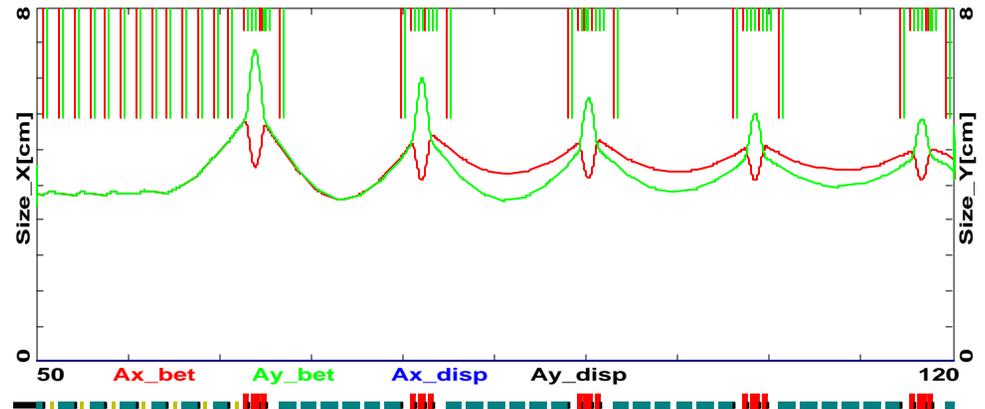
- Synchrotron motion suppresses the sag of particle energy at bunch edges
- No longitudinal emittance increase during acceleration
- Design of Cryomodules is based on the Project X and ILC technologies
  - ◆ Two types of cryomodules
    - With solenoidal focusing: 1 solenoid per cavity
    - With Triplet focusing: 6 cavities per triplet
  - ◆ All but 2 solenoids and all but 2 triplets are connected serially



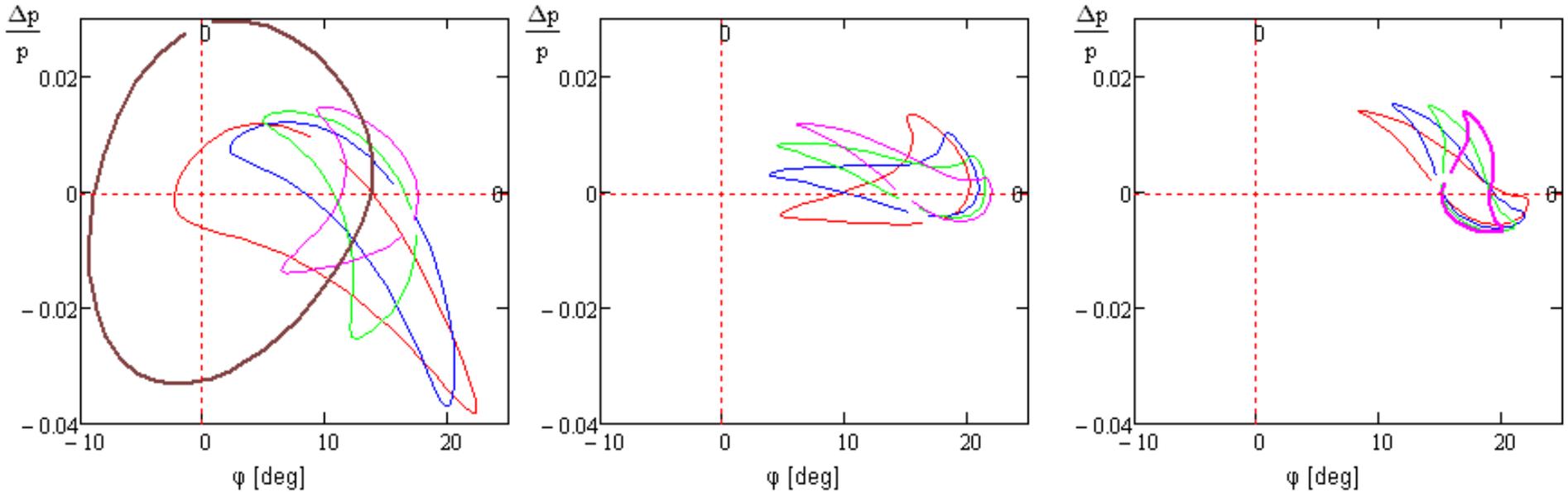
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# Acceleration in Recirculator (based on Proj. X linac)



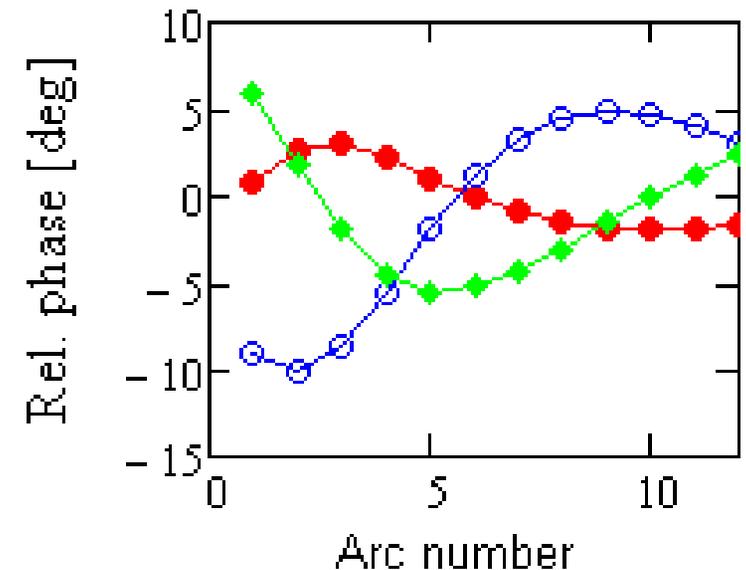
*Phase spaces at the beginning and at the end of each linac end for  $3\sigma$  beam envelopes*

- Adjustments of  $M_{56}$  and accelerating phases for each arc and linac pass control the momentum spread and bunch length

$$M_{56} := (10 \ 25 \ 30 \ 35 \ 35 \ 30 \ 27 \ 25 \ 25 \ 25 \ 25 \ 25)^T \text{ cm}$$

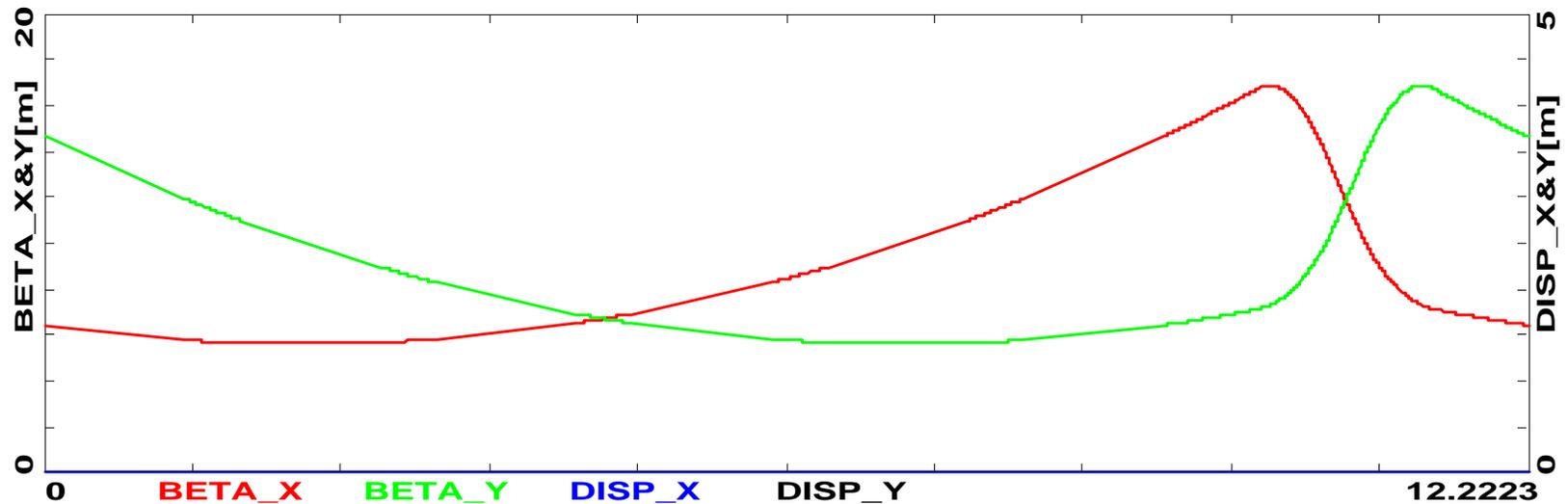
$$\phi_a := -(8 \ 13 \ 14 \ 15 \ 17 \ 17 \ 17 \ 17 \ 17 \ 17 \ 17 \ 17)^T \text{ deg}$$

- Negligible longitudinal growth for major part of particles (within  $2\sigma$ )

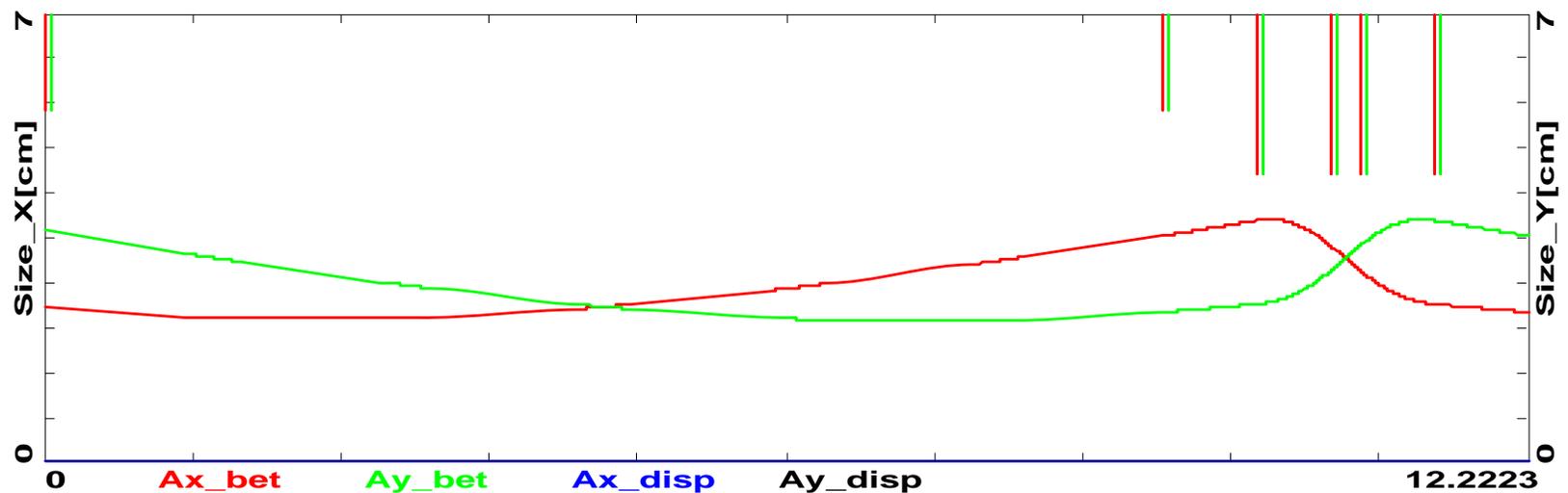


# Acceleration in Recirculator (continue)

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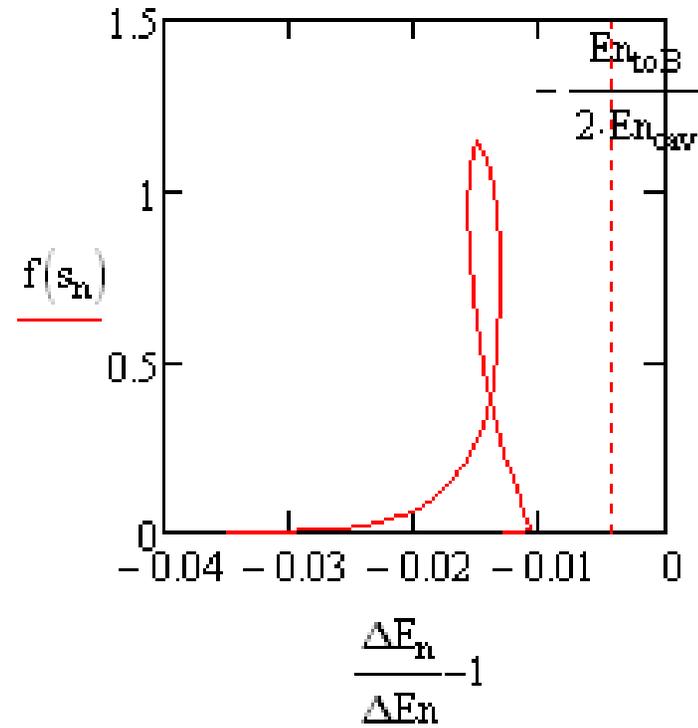
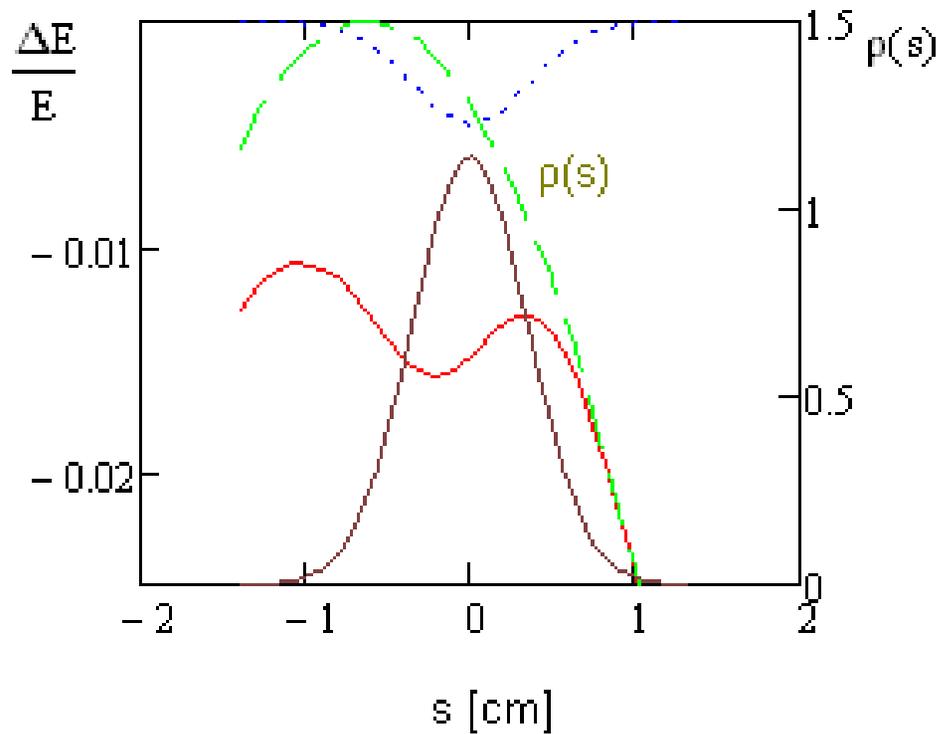


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*Beta-functions and  $3\sigma$  beam envelopes for the first pass period*

# Beam Loading

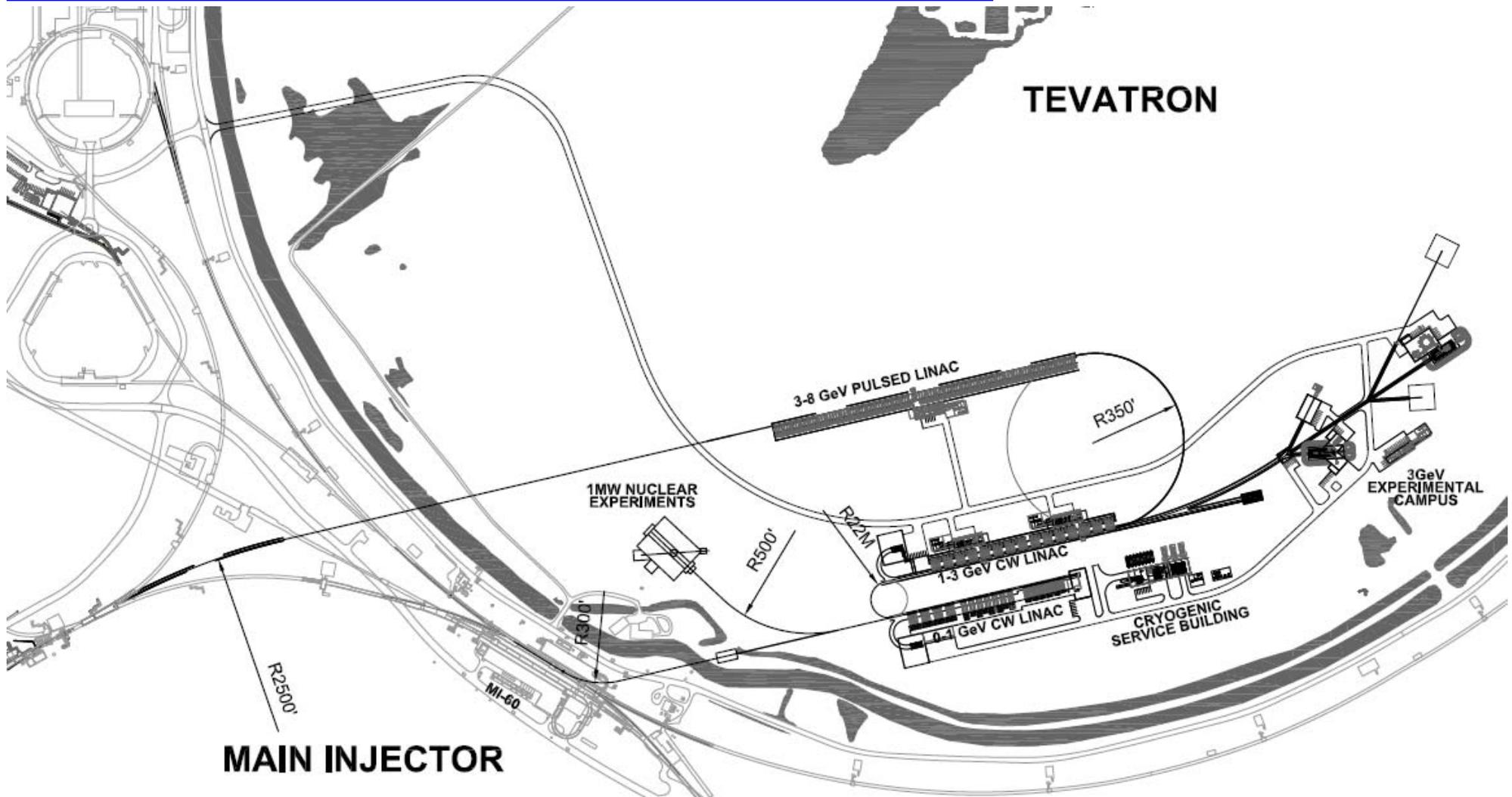


*Beam loading for single pass of  $6 \cdot 10^{11}$  particles per bunch;*

$$\phi_{acc} = 4.9 \text{ deg}, \sigma_s = 3.5 \text{ mm} \Rightarrow \sigma_E = 0.15\%$$

- Single bunch takes 0.82% out of energy stored in a cavity
- 12 passes + ( $\mu^+$  &  $\mu^-$ ) yield 20% of energy taken by the beam
  - ◆ 10% accelerating gradient droop to the last pass
- Synchrotron motion in Recirculator additionally reduces momentum spread
  - ◆ Longitudinal auto-phasing reduces the dependence of final beam energy on the bunch intensity

# Project X and Higgs Factory Siting



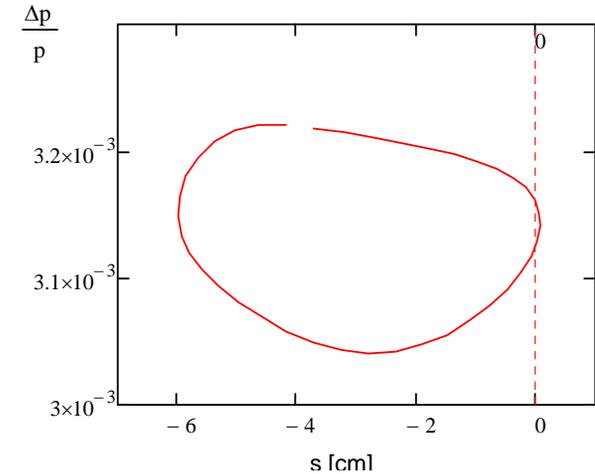
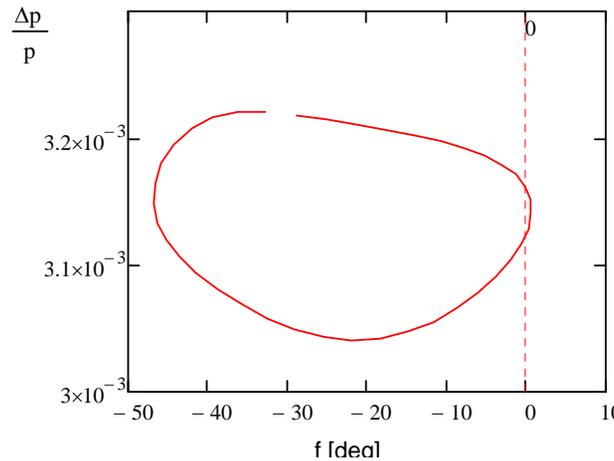
- Recently adopted Project X siting fits well to the Higgs factory needs
  - ◆ Cost reduction for the first stage
  - ◆ Enough place for Recirculator arcs and the rest of the Higgs factory
  - ◆ Penalty: Emittance growth in arcs; isochronicity helps but the beam space charge induces the emittance growth

# Beam Debunching

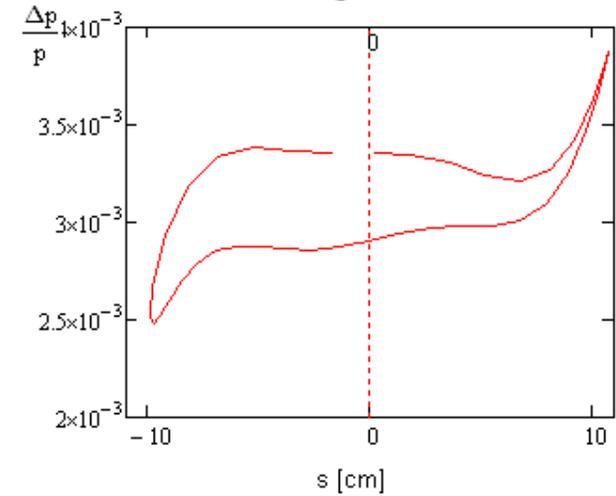
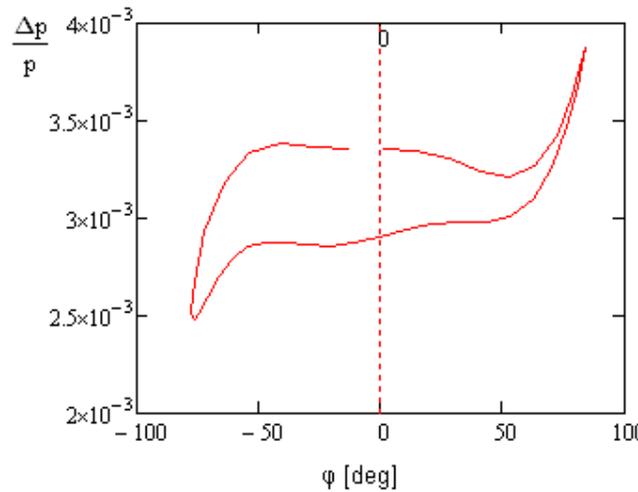
■ Beam debunching is used to reduce momentum spread

- ◆ For given longitudinal emittance of 1.5 mm one can use the same 650 MHz cryomodules with additional 1.3GHz cryomodules for non-linearity compensation. It also requires an arc with large value of  $M_{56}$ .
- ◆ That results in the rms length of  $\sim 3$  cm, and momentum spread of  $\sim 7 \cdot 10^{-5}$ .
- ◆ Twice smaller value of  $\Delta p/p$  can be achieved with twice larger  $M_{56}$  and linacs with two times smaller frequency and approximately the same voltage

1s longitudinal phase space after debunching



3σ longitudinal phase space after debunching



Longitudinal phase spaces

$(\Delta p/p, \phi)$  and  $(\Delta p/p, s)$  after debunching

$M_{56}=10$  m,  $V_{(650 \text{ MHz})}=0.64$  GeV,  $V_{(1.3 \text{ MHz})}=0.1$  GeV

# Conclusions

- There is a considerable synergy between Project X and Higgs factory ( $L \sim 5 \cdot 10^{29} \text{ cm}^{-2} \text{ s}^{-1}$ )  
if the pulsed Project X linac is based on 650 MHz technology and its cavities are spaced by integer number of cell length
  - ◆ The linac can be used for acceleration of  $\sim 6 \cdot 10^{11}$  muons per bunch for both  $\mu^+$  and  $\mu^-$  bunches with 12 pass recirculator
  - ◆ Only modest upgrade of pulsed linac RF will be required
    - to  $\sim 1.5 \text{ MW}$  ( $0.6 \text{ MW}$  for acceleration of muons and  $1 \text{ MW}$  for acceleration of protons)
    - $\sim 20\%$  duty factor (13 ms proton beam pulse,  $f_{\text{rep}} = 10 \text{ Hz}$ )
    - No upgrade for CW part
  - ◆ Very significant price reduction for the Higgs factory or neutrino factory
- Technology developed for CW Project X linac well suits for the muon linac (3.1 GeV)
  - ◆ Cavities, solenoids, etc.